

# Current status of the light neutralino thermal dark matter in the pMSSM

based on PRL 131 (2023) 1, 011802 and arXiv:2312.xxxxx

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UNIVERSITÄT **BONN**



# Dark Matter

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**Multiple  
evidences**

Galaxy Rotation Curves

Bullet Cluster

Gravitational Lensing

Cosmic Microwave Background

**No idea about mass, spin and couplings**

One possible DM candidate:

the **lightest neutralino** in the Minimal Supersymmetric Standard Model (MSSM)  a well-motivated BSM model

**How does this very conventional dark matter candidate stand against the recent experimental results?**

# Lightest Neutralino in the MSSM

## Extending SM to MSSM

**Higgs sector:** 2 Higgs doublets in MSSM:  $H_u, H_d$   
5 Higgs bosons:  $h, H, A, H^\pm$

## Supersymmetry (SUSY):

Weyl fermion  $\leftrightarrow$  complex scalar      fermions  $\leftrightarrow$  sfermions

complex scalar  $\leftrightarrow$  Weyl fermion      Higgs bosons  $\leftrightarrow$  higgsinos

gauge bosons  $\leftrightarrow$  Weyl fermion      gauge bosons  $\leftrightarrow$  gauginos

## Electroweakino sector:

Lightest neutralino

$\tilde{B}, \tilde{W}, \tilde{H}_u, \tilde{H}_d \rightarrow \tilde{B}, \tilde{W}^0, \tilde{H}_u^0, \tilde{H}_d^0 \rightarrow$  4 neutralinos:  $\tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_4^0$   
 $\tilde{W}^+, \tilde{H}_u^+, \tilde{W}^-, \tilde{H}_d^- \rightarrow$  4 charginos:  $\tilde{\chi}_1^\pm, \tilde{\chi}_2^\pm$   
mixing

# Lightest Neutralino dark matter in the MSSM

## R-parity

$R$ -parity is defined as

$$R = (-1)^{3(B-L)+2s}$$

$B$ : baryon number

$L$ : lepton number

$s$ : spin

SM particles: even under  $R$ -parity

Superpartners: odd under  $R$ -parity

In  $R$ -parity conserving (RPC) scenario

Lightest Supersymmetric Particle (LSP) is stable

can be dark matter if neutral

# Lightest Neutralino **dark matter** in the MSSM

## \* LSP in RPC SUSY?

Focus on parameter space where the LSP contributes to the invisible decay of SM Higgs Boson

Light neutralino, where  $M_{\tilde{\chi}_1^0} \lesssim M_h/2$

Dominantly **Bino** due to LEP limit on chargino mass

$$M_{\tilde{\chi}_1^\pm} \gtrsim 103 \text{ GeV}$$

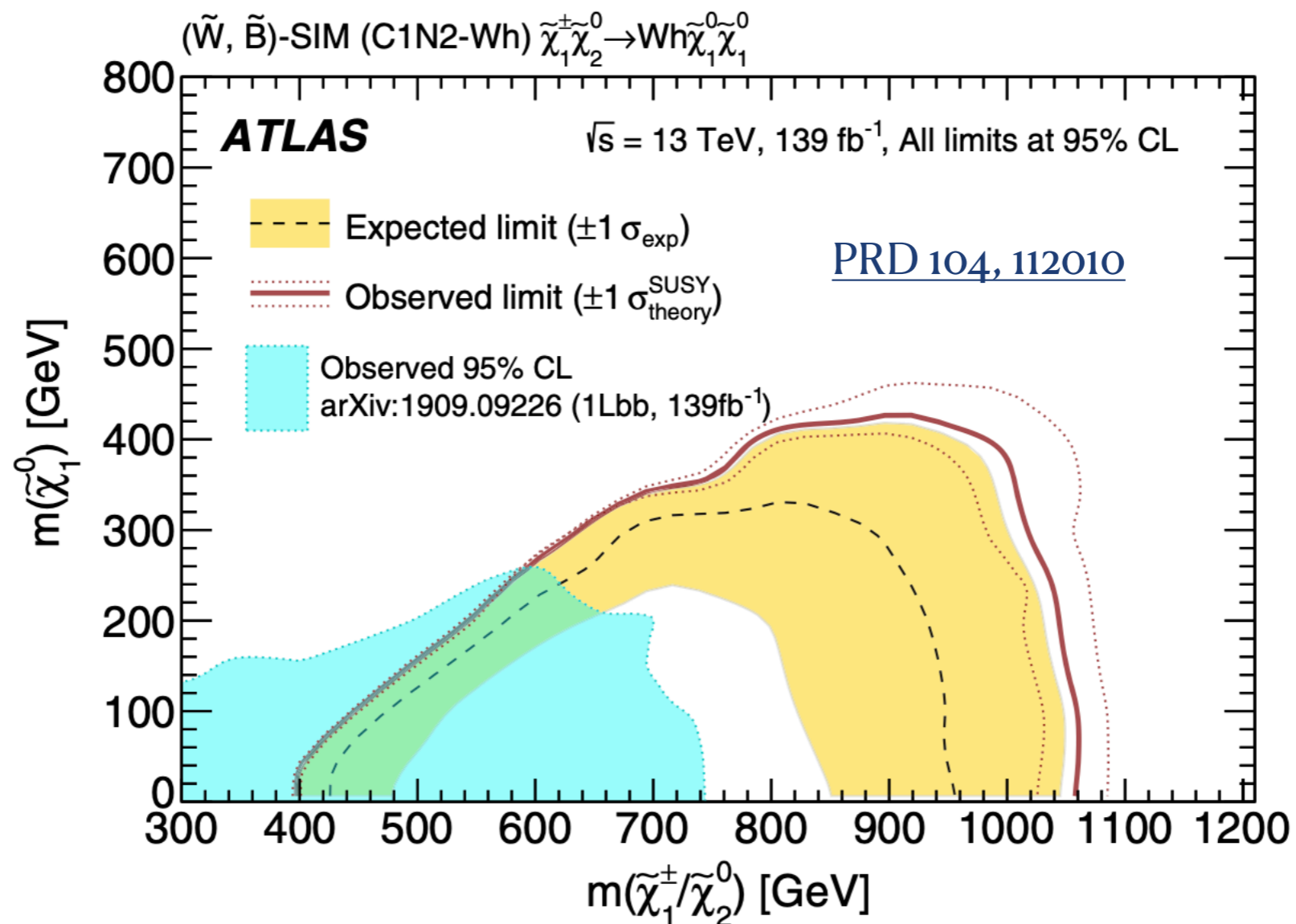
[arXiv:hep-ex/0401026](https://arxiv.org/abs/hep-ex/0401026)

# Lightest Neutralino **dark matter** in the MSSM

## \* NLSP?

NLSP: Next-to Lightest Supersymmetric Particle

Mostly **Higgsino** due to strong limits for Wino NLSP



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*coupling of the LSP with  $Z$  and  $h$  bosons depends on the Bino, Wino, and Higgsino components in it*

$$g_{Z\tilde{\chi}_1^0\tilde{\chi}_1^0} = \frac{g}{2\cos\theta_W} \left( |N_{13}|^2 - |N_{14}|^2 \right)$$

$$g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0} = -g \left( N_{12} - \tan\theta_W N_{11} \right) \left( \sin\alpha N_{13} + \cos\alpha N_{14} \right)$$

$N_{1i}$  :  $i$ th component in  $\tilde{\chi}_1^0$ , where  $(\sin\beta N_{14} - \cos\beta N_{13}), M_A \gg M_Z$   
 $i = \tilde{B}, \tilde{W}^0, \tilde{H}_u^0, \tilde{H}_d^0$

**Higgsino** component required in the LSP for its coupling to  
 $Z$  and  $h$  bosons

# Lightest Neutralino dark matter in the MSSM

## \* NLSP?

NLSP: Next-to Lightest

Mostly Higgsino

coupling of the LSP

$$g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0}$$

### Previous works

Chattopadhyay, et al., PRD 82, 075013 (2010)

Barman, et al., PRD 95, 095018 (2017)

Pozzo, Zhang, PLB 789 (2019) 582–591

Barman, et al., Eur. Phys. J. Spec. Top. 229, 3159–3185 (2020)

Beekveld, et al., SciPost Phys. 11, 049 (2021)

*and many more...*

**New data!**

$$g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0} = \frac{g}{2} \cos\beta N_{13}, \quad M_A \gg M_Z$$

Higgsino component required in the LSP for its coupling to  $Z$  and  $h$  bosons



# The pMSSM Parameter Space

10 parameters scanned

Slepton masses fixed at 2 TeV

1st and 2nd generation squark masses fixed at 5 TeV

$$30 \text{ GeV} < M_1 < 100 \text{ GeV}, \quad 1 \text{ TeV} < M_2 < 3 \text{ TeV},$$

$$100 \text{ GeV} < |\mu| < 2 \text{ TeV}, \quad 2 < \tan \beta < 50,$$

$$100 \text{ GeV} < M_A < 5 \text{ TeV}, \quad 3 \text{ TeV} < M_{\tilde{Q}_{3L}} < 20 \text{ TeV},$$

$$3 \text{ TeV} < M_{\tilde{t}_R} < 20 \text{ TeV}, \quad 3 \text{ TeV} < M_{\tilde{b}_R} < 20 \text{ TeV},$$

$$-20 \text{ TeV} < A_t < 20 \text{ TeV}, \quad 2 \text{ TeV} < M_3 < 5 \text{ TeV},$$

$$M_{\tilde{Q}_{1,2L}} = M_{\tilde{u}_{1,2R}} = M_{\tilde{d}_{1,2R}} = 5 \text{ TeV}, \quad A_{u/d/c/s/b} = 0,$$

$$M_{\tilde{L}_{1,2,3L}} = M_{\tilde{e}_{1,2,3R}} = 2 \text{ TeV}, \quad A_{e/\mu/\tau} = 0.$$

$M_1$  bino mass

$M_2$  wino mass

$\mu$  higgsino mass

$\tan\beta$  ratio of vevs

$M_A$  pseudoscalar  
mass

$M_{\tilde{Q}_{3L}}, M_{\tilde{t}_R}, M_{\tilde{b}_R}$

3rd generation  
squark mass

$A_t$  stop trilinear  
coupling

$M_3$  gluino mass

Both  $\mu > 0$  and  $\mu < 0$   
scenarios studied  
separately

Particle spectrum generated using  
FeynHiggs 2.18.1

## LEP, Flavor

### LEP constraints

invisible decay of Z-boson  
from new physics

$$\Gamma_{\text{inv}}^{\text{new}} < 2 \text{ MeV}$$

ALEPH, DELPHI, L3, OPAL, [Phys. Rept. 427 \(2006\) 257–454](#)

chargino mass

$$m_{\chi_{\pm}^1} > 103 \text{ GeV}$$

OPAL, [EPJC 35, 1–20 \(2004\)](#)

cross-section of associated production  
of neutralinos in final states with jets

$$\begin{aligned} & \sigma(e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0) \times \text{Br}(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 + \text{jets}) \\ + & \sigma(e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_3^0) \times \text{Br}(\tilde{\chi}_3^0 \rightarrow \tilde{\chi}_1^0 + \text{jets}) < 0.1 \text{ pb} \end{aligned}$$

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# Current Constraints on the Parameter Space

MicrOMEGAS 5.2.13

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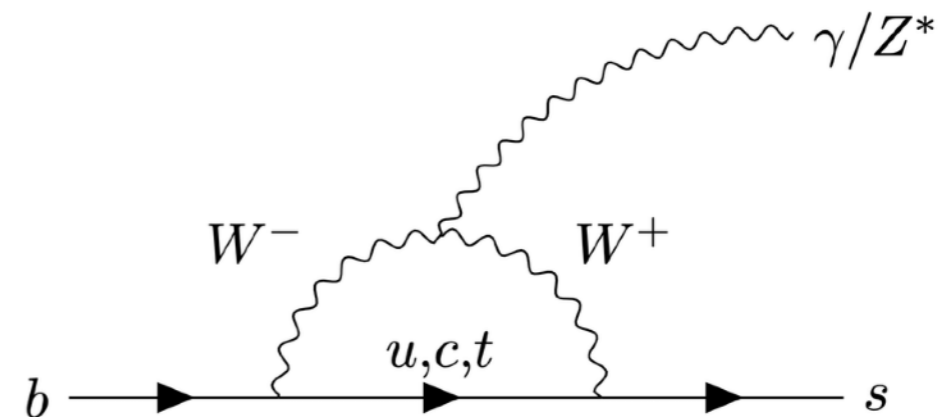
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OPAL, [EPJC 35, 1–20 \(2004\)](#)

## LEP, Flavor

## Flavor observables

- \* Rare processes in SM
- \* Might receive contribution from MSSM
- \* Precise measurement of the branching of these processes constrain the MSSM parameter space



$$3.00 \times 10^{-4} < \text{Br}(b \rightarrow s \gamma) < 3.64 \times 10^{-4}$$

HFLAV, [Eur. Phys. J. C 77, 895 \(2017\)](#)

$$1.66 \times 10^{-9} < \text{Br}(B_s \rightarrow \mu^+ \mu^-) < 4.34 \times 10^{-9}$$

CMS & LHCb, [Nature 522, 68–72 \(2015\)](#)

$$0.78 < (\text{Br}(B \rightarrow \tau \nu))_{\text{obs}} / (\text{Br}(B \rightarrow \tau \nu))_{\text{SM}} < 1.78$$

Belle, [PRD 82, 071101\(R\)](#)

# Current Constraints on the Parameter Space

## Higgs constraints

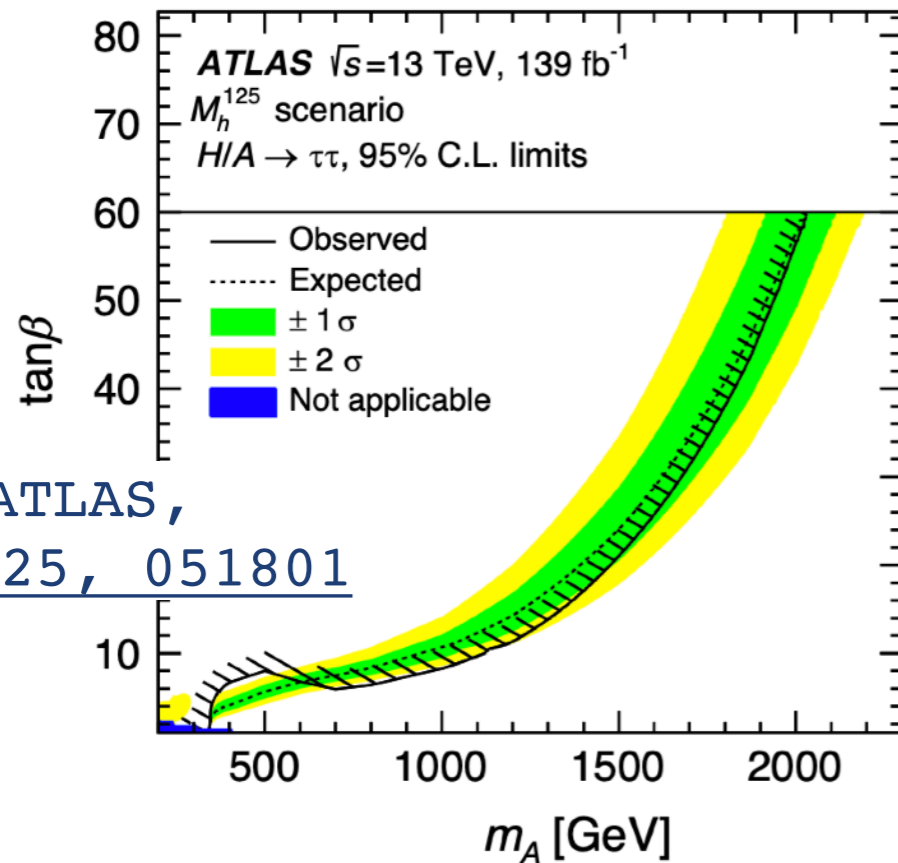
### Observed Higgs mass

$$122 \text{ GeV} < m_h < 128 \text{ GeV}$$

FeynHiggs 2.18.1

### Heavy Higgs searches

HiggsBounds 5.10.0



### Higgs signal strength

$$\mu = \frac{(\text{Production}_{\text{mode}} \times \text{Branching}_{\text{mode}})_{\text{obs}}}{(\text{Production}_{\text{mode}} \times \text{Branching}_{\text{mode}})_{\text{SM}}}$$

HiggsSignal 2.6.2

### Invisible decay of the Higgs Boson

$$\text{Br}(h \rightarrow \text{invisible}) < 0.11$$

ATLAS, [ATLAS-CONF-2020-052](#)

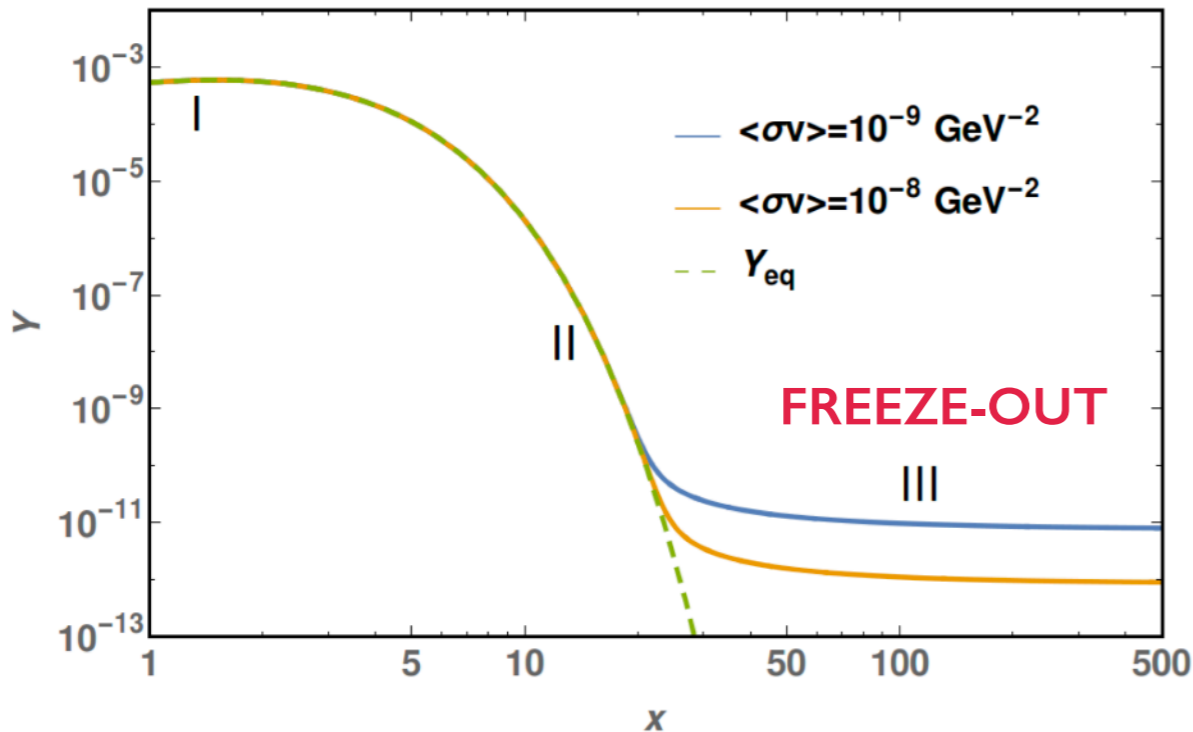
# Current Constraints on the Parameter Space

MicrOMEGAS 5.2.13

## Dark matter constraints

### Relic Density

DM in thermal equilibrium with other SM particles in the early Universe



$$x = \frac{m}{T}, Y = \frac{n}{s}$$

$$s = \frac{2\pi^2}{45} g_{*s} T^3$$

$m$  : mass of the particle  
 $T$  : temperature of the thermal bath  
 $n$  : number density of the particle  
 $s$  : entropy density of the thermal bath

Observed relic density of Dark Matter:

$$\Omega_{\text{DM}}^{\text{obs}} h^2 = 0.120 \pm 0.001 \quad \text{PLANCK collaboration}$$

$$\Omega_{\text{LSP}} h^2 \lesssim 0.122$$

If underabundant,  
multi-component DM

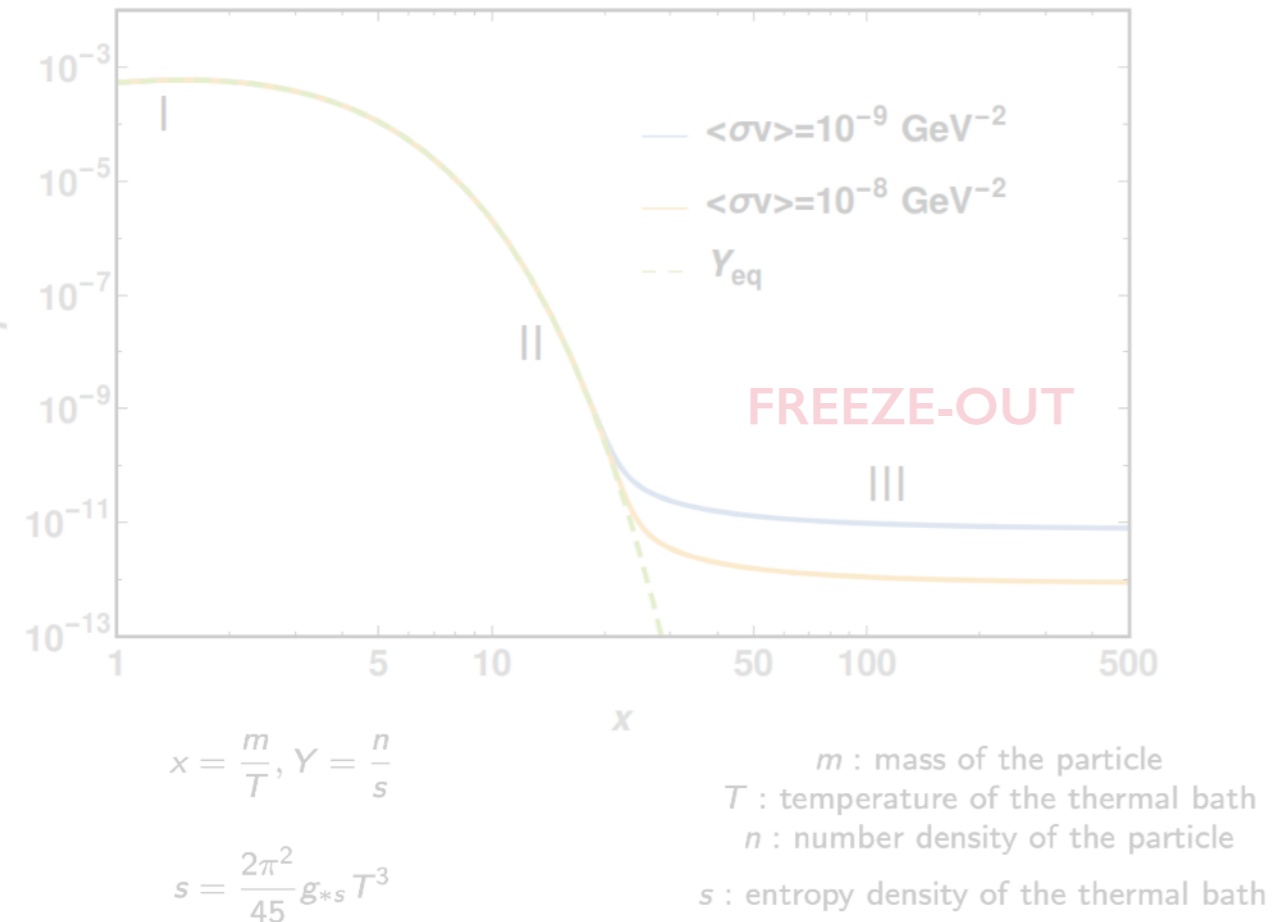
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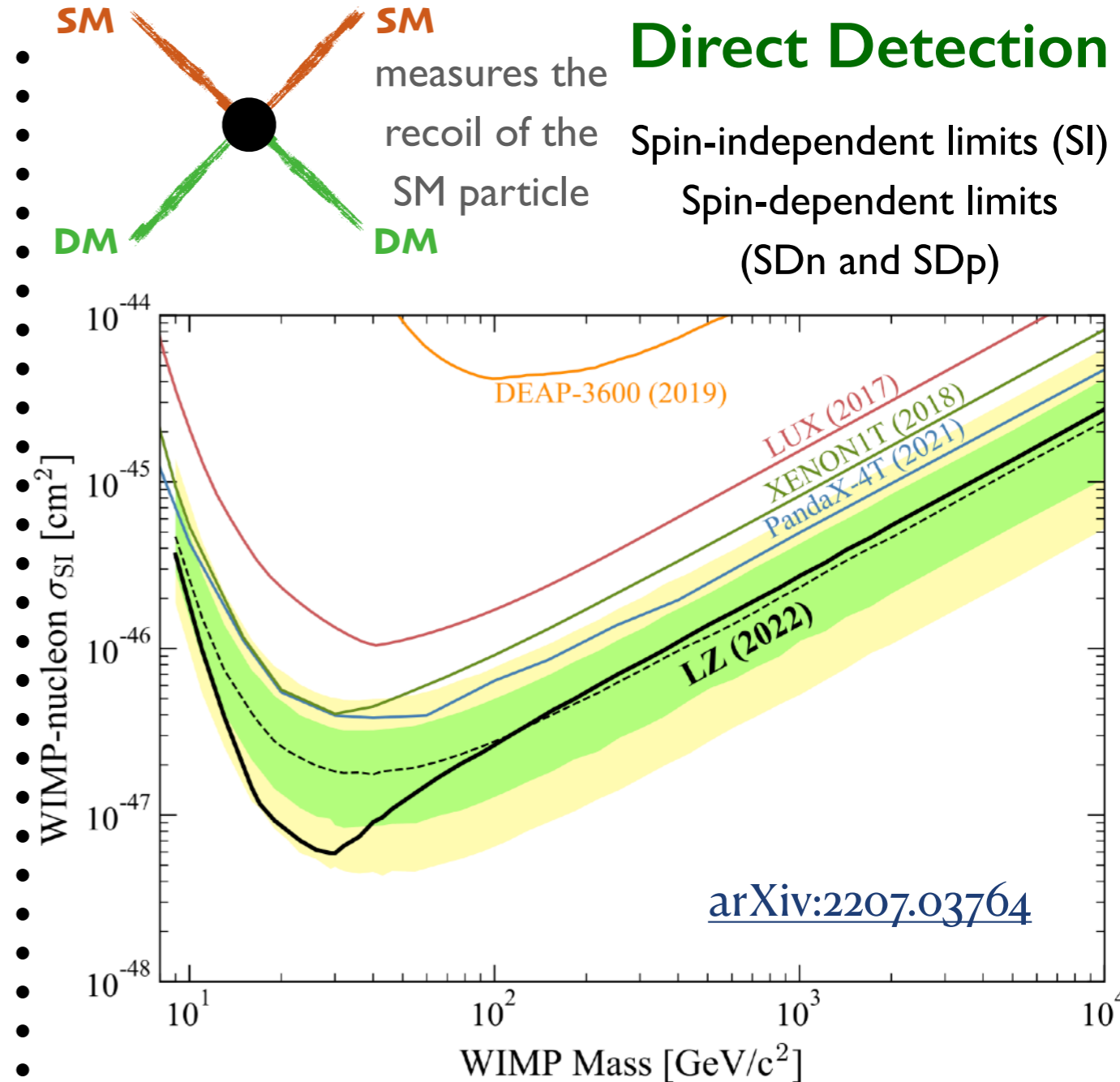
$$\Omega_{\text{LSP}} h^2 \lesssim 0.122$$

If underabundant, multi-component DM

### Direct Detection

measures the recoil of the SM particle

Spin-independent limits (SI)  
Spin-dependent limits (SDn and SDp)



If underabundant,

$$\sigma_{\text{DD}} \rightarrow \sigma_{\text{DD}} \times \xi$$

$$\xi = \frac{\Omega_{\text{LSP}}}{0.120}$$

# Current Constraints on the Parameter Space

## Electroweakino constraints

results of direct searches for chargino and neutralino at the ATLAS and CMS experiments of the LHC

$$pp \rightarrow \tilde{\chi}_1^\pm \tilde{\chi}_2^0 / \tilde{\chi}_1^\pm \tilde{\chi}_3^0$$

$$\tilde{\chi}_1^\pm \rightarrow W^\pm \tilde{\chi}_1^0$$

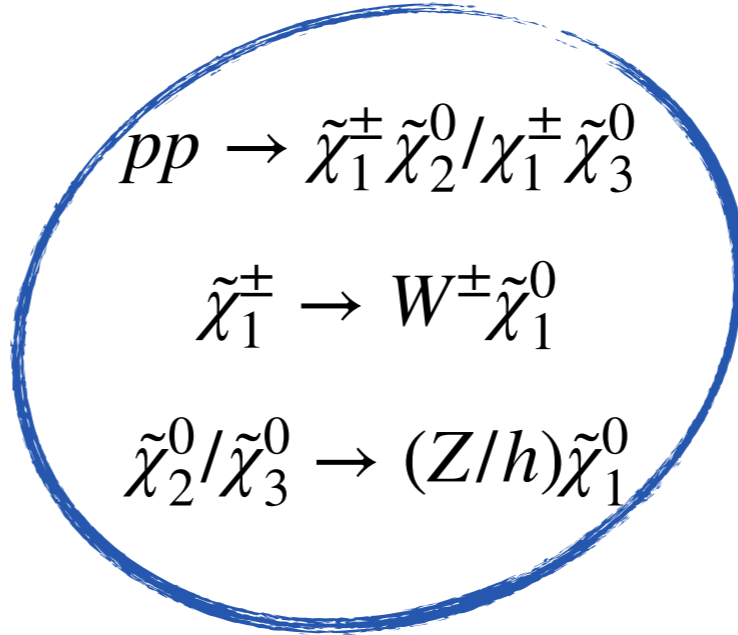
$$\tilde{\chi}_2^0 / \tilde{\chi}_3^0 \rightarrow (Z/h) \tilde{\chi}_1^0$$

Leptonic decay modes of  $W/Z/h$ : being **cleaner** have been used in the past, like  $3l + \text{MET}$  analysis  
Low branching - sensitive to lighter NLSPs

# Current Constraints on the Parameter Space

## Electroweakino constraints

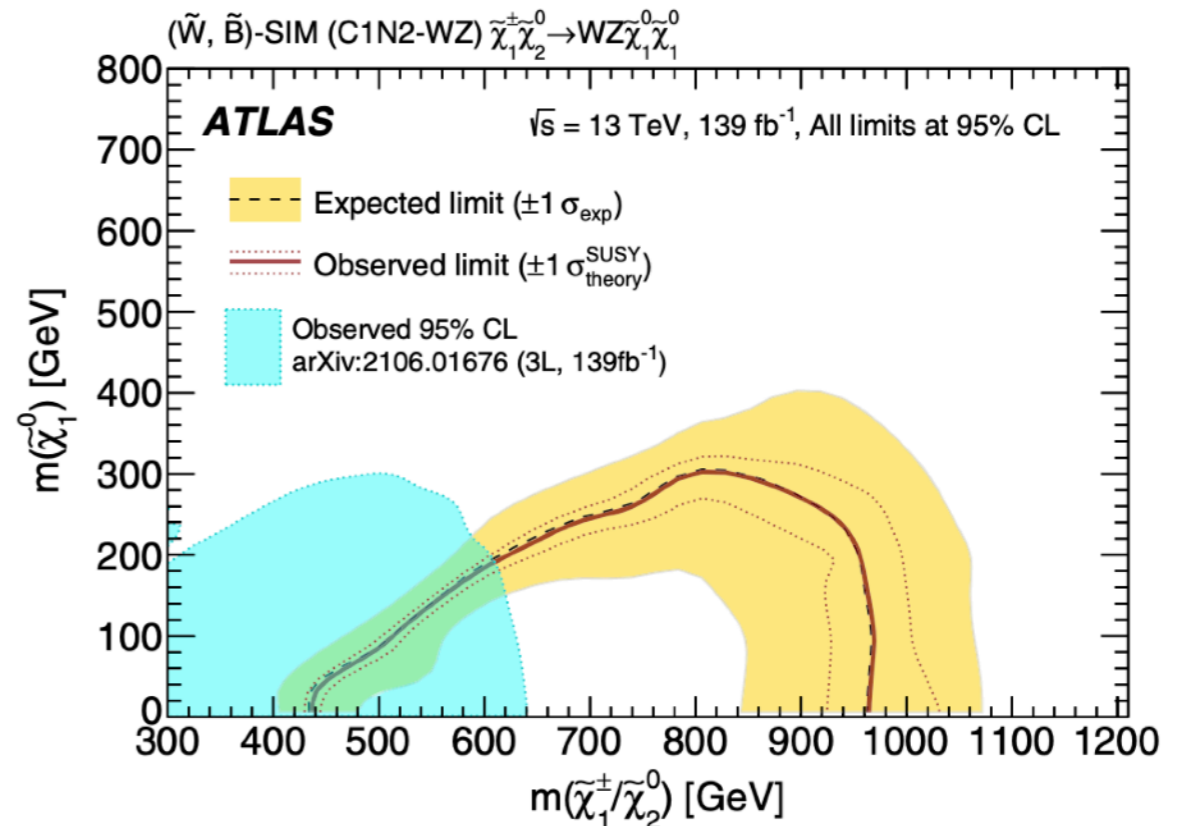
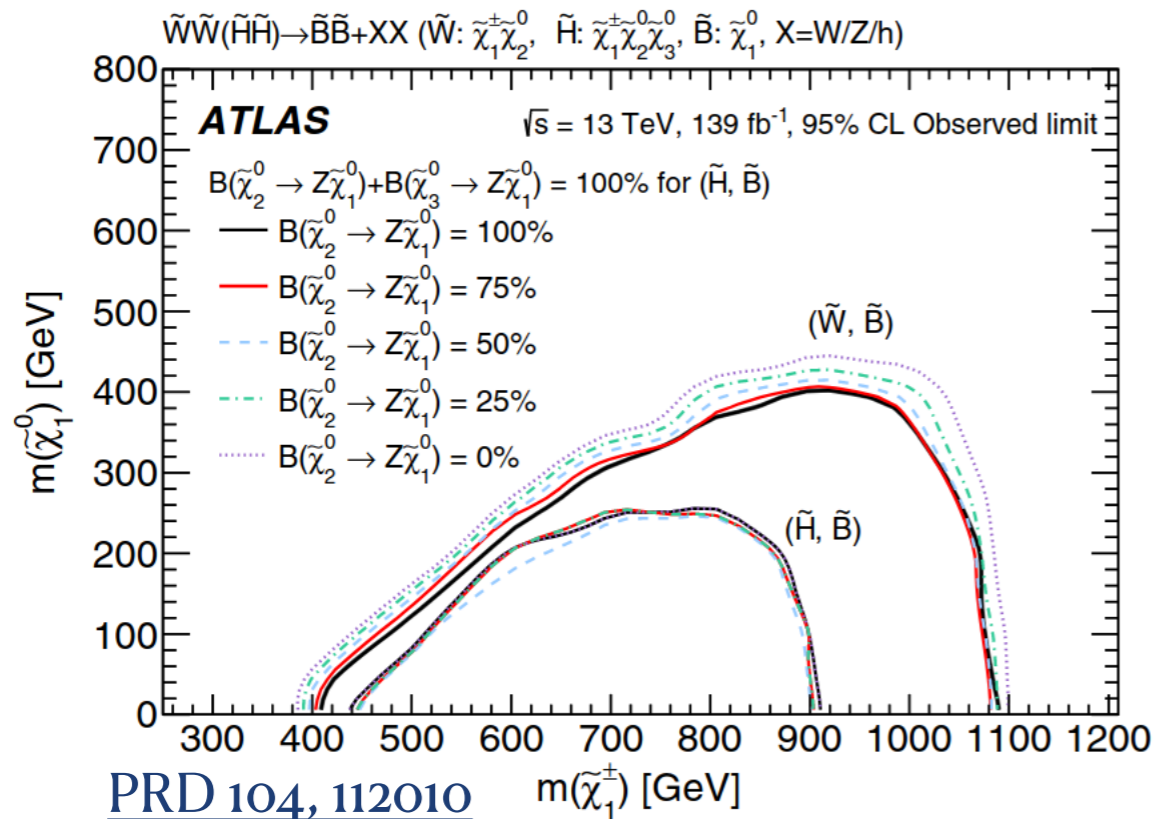
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Leptonic decay modes of  $W/Z/h$ : being **cleaner** have been used in the past, like **3l + MET** analysis  
**Low branching - sensitive to lighter NLSPs**

Recently, **hadronic final states** are also being analysed

⇒ **increase sensitivity to heavier NLSPs**

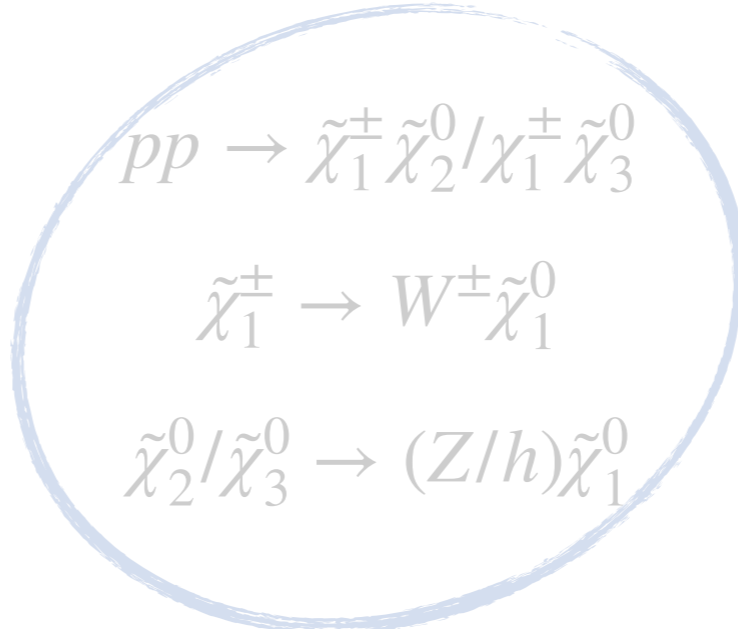




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## Electroweakino constraints

results of direct searches for chargino and neutralino at the ATLAS and CMS experiments of the LHC



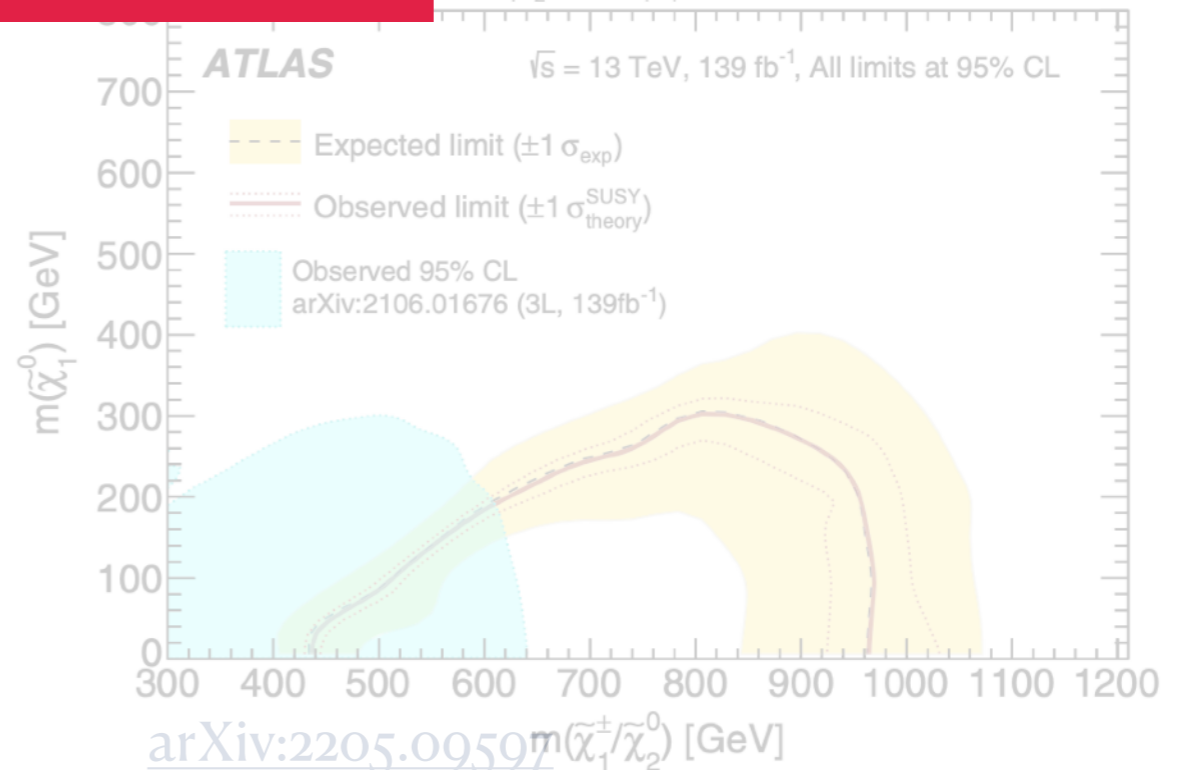
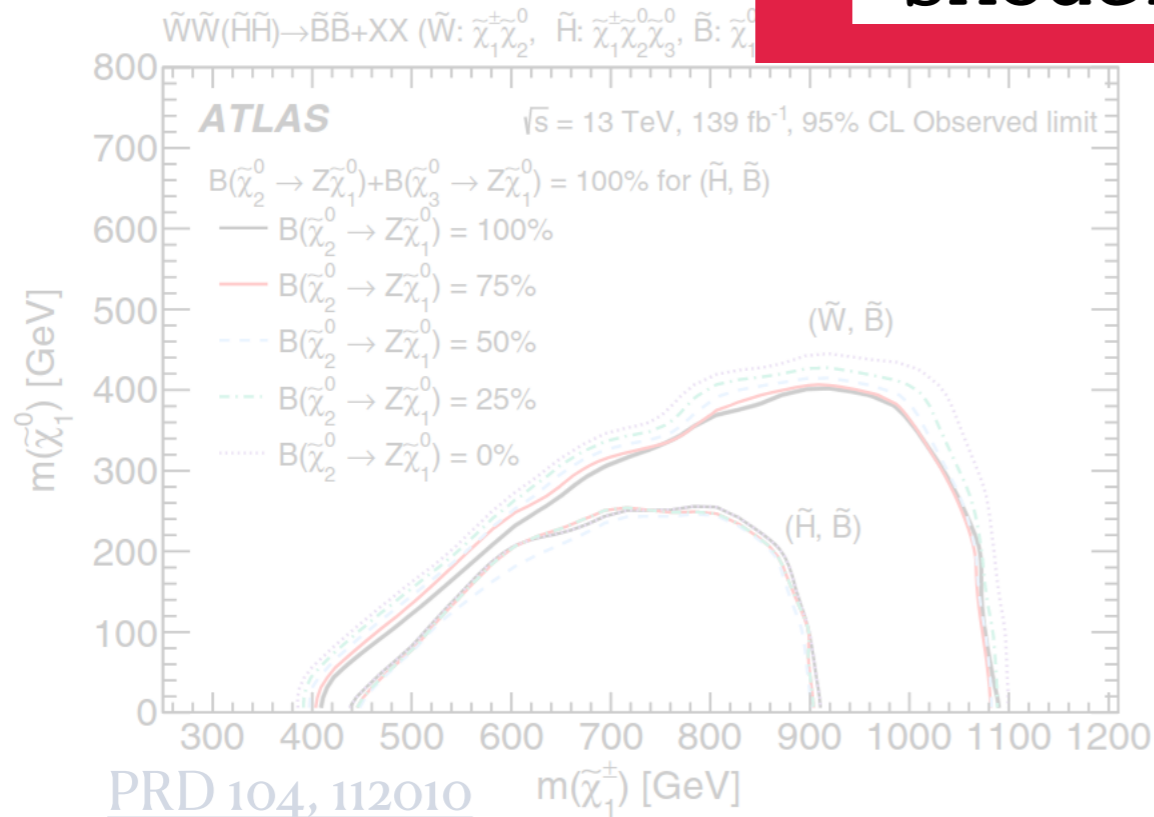
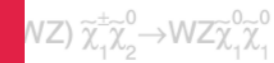
Leptonic decay modes of  $W/Z/h$ : being cleaner have been used in the past, like  $3l + MET$  analysis  
 Low branching - sensitive to lighter NLSPs

Recently, hadronic decays are being analysed

Implemented using SModelS 2.2.1

being analysed

NLSPs



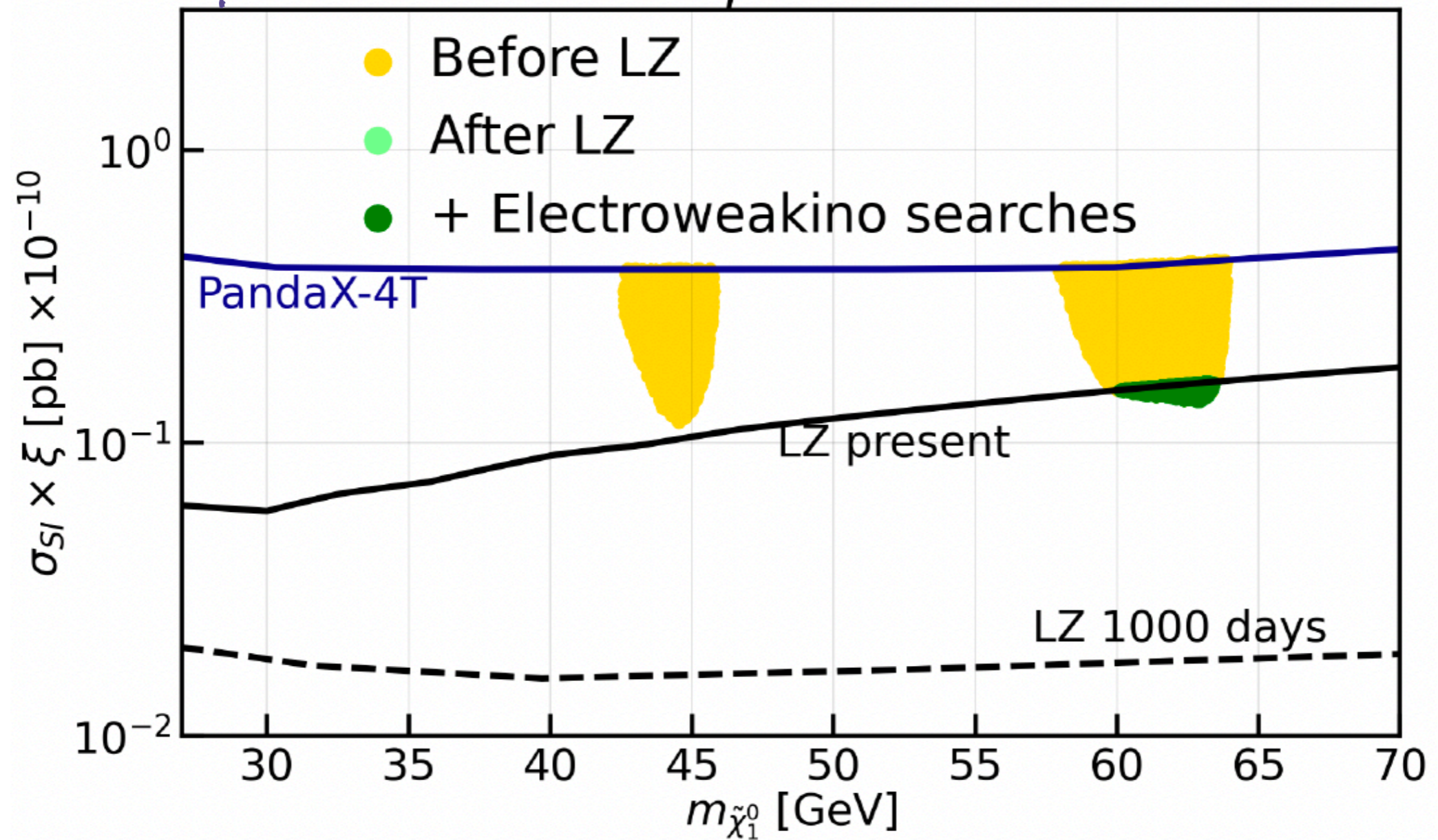
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# Results

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# The Positive $\mu$ Scenario

Spin-independent DD Limit  $\mu > 0$

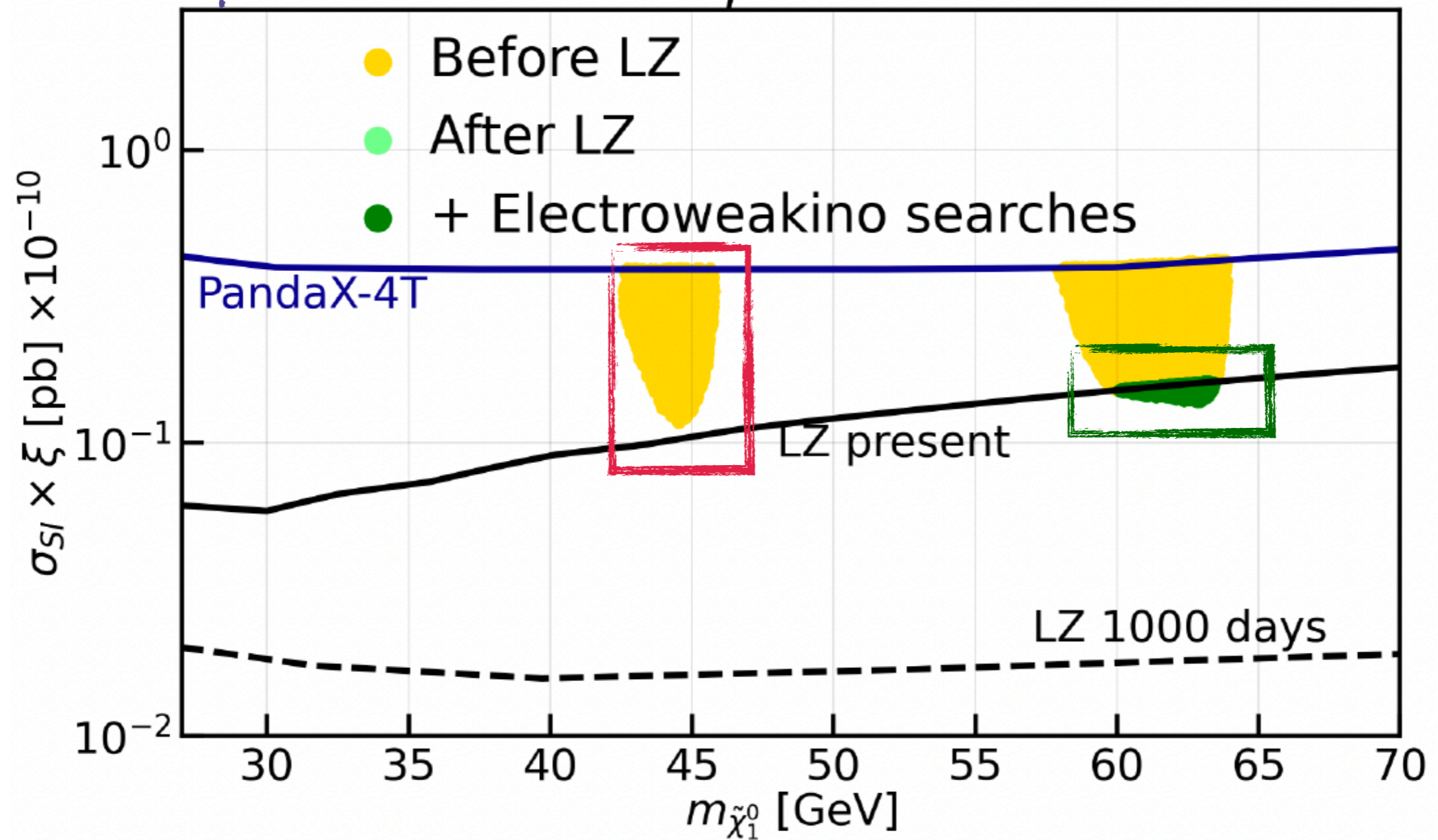


DD limits restrict allowed parameter space to  $Z$  and  $h$  funnel regions since here relic density can be satisfied even with smaller coupling due to resonance enhancement

**Before LZ:** constraints from LEP, flavor, Higgs constraints, relic density and the DD experiments **XENON-1T**, **PICO-60** and **PandaX-4T**

# The Positive $\mu$ Scenario

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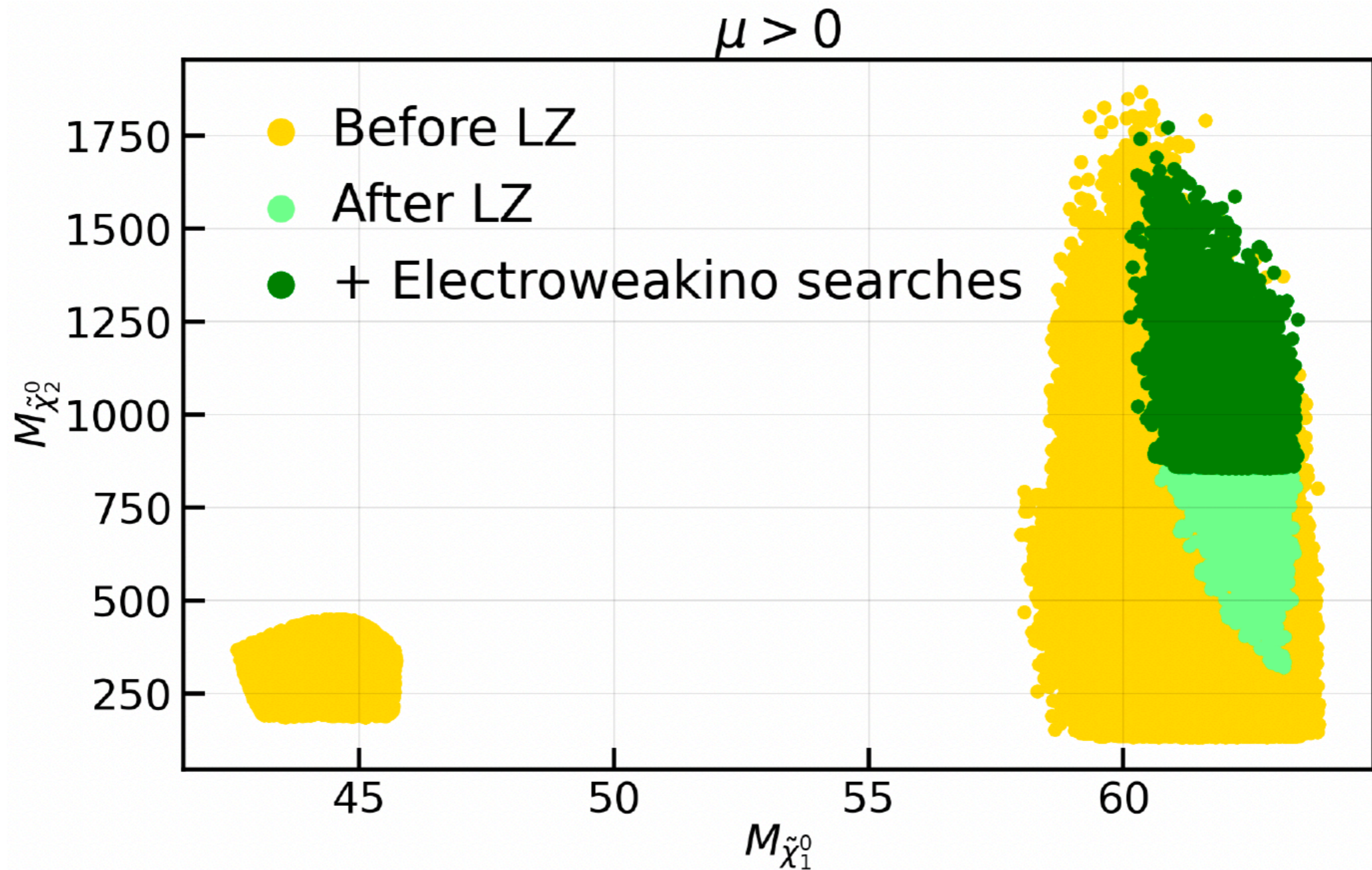
Z-funnel excluded

Allowed region in  $h$ -funnel

Well within the reach of the full LZ data

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# The Positive $\mu$ Scenario



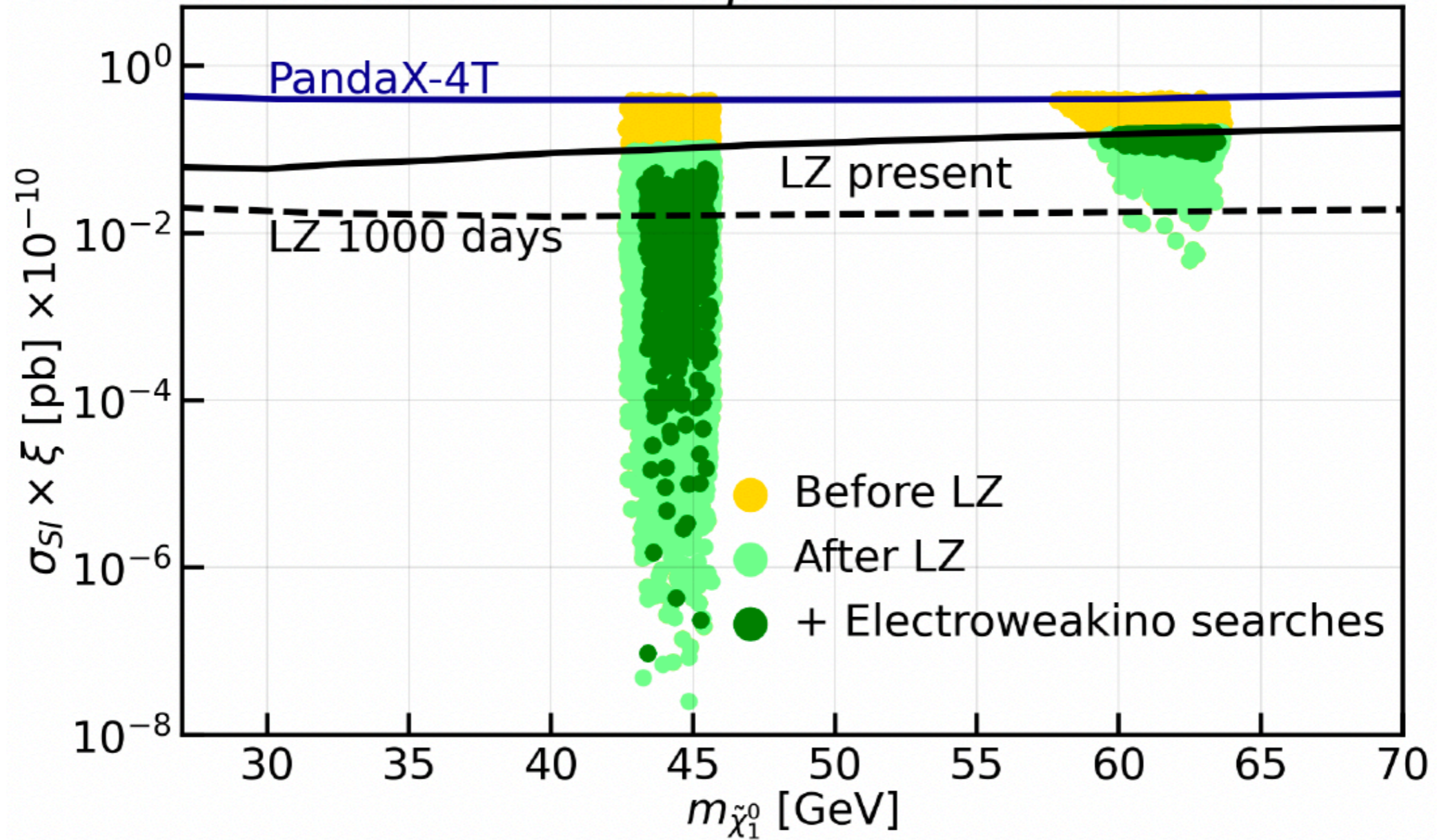
Higgsinos heavier than  
 $\sim 850$  GeV allowed from  
electroweakino searches

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# The Negative $\mu$ Scenario

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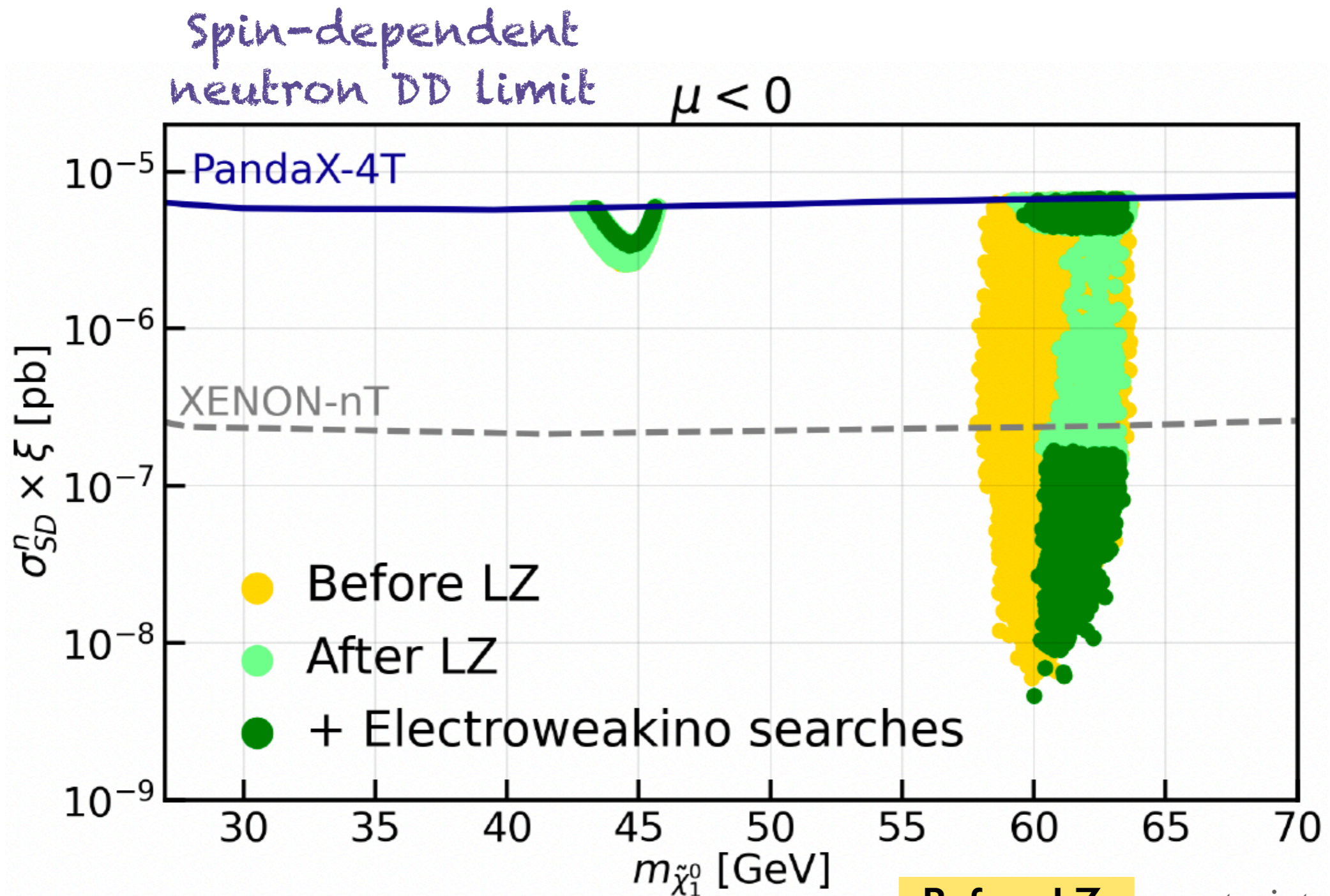
$\mu < 0$



Allowed regions in both  $Z$  and  $h$  funnels  
 $h$ -funnel well within the reach of the full  
LZ data

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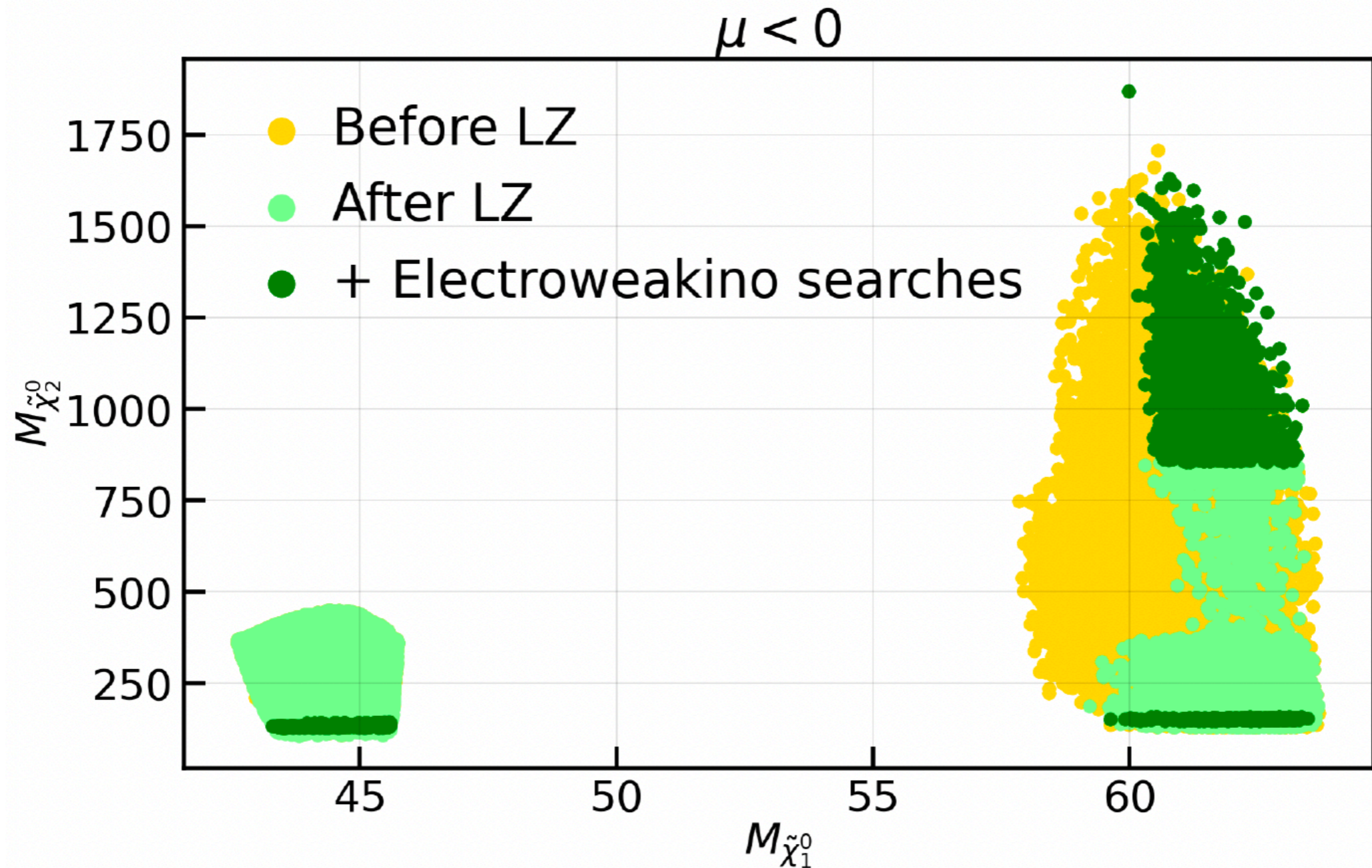
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Z-funnel well within the reach of  
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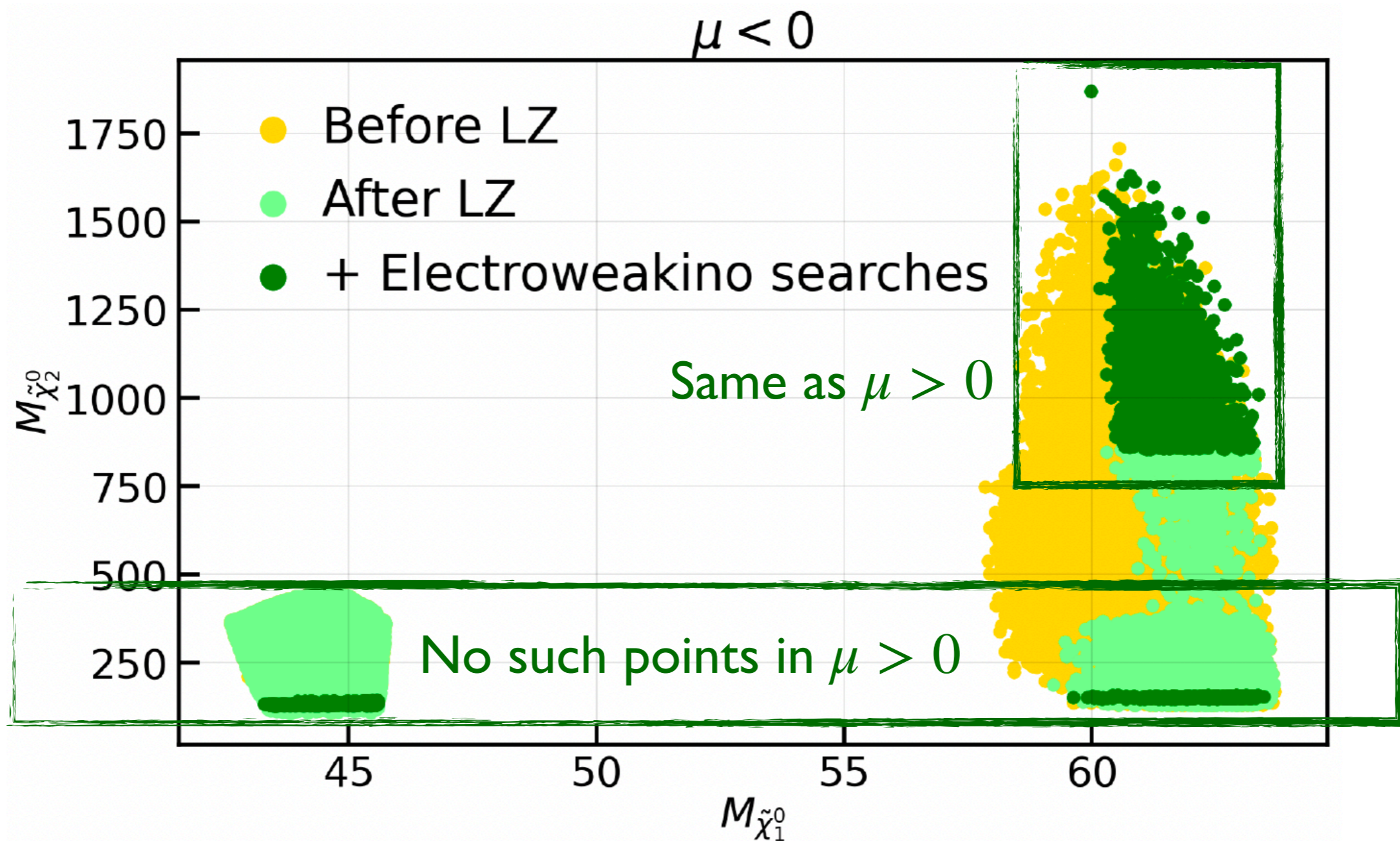
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# The Negative $\mu$ Scenario



**Before LZ:** constraints from LEP, flavor, Higgs constraints, relic density and the DD experiments **XENON-1T**, **PICO-60** and **PandaX-4T**

# Light higgsinos: impact of LZ dependent on the sign of $\mu$

**LZ limits the SI DD cross-section**

Both  $h$  and  $H$  contribute to this

$\mu > 0$  tan $\beta$  enhanced  $\mu < 0$  when  $g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0} < 0$

These contributions **constructively interfere** for down type quarks

These contributions **destructively interfere** for down type quarks

Even for same  $g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0}$  coupling, the SI DD cross-section increases for  $\mu > 0$  and decreases for  $\mu < 0$  for high tan $\beta$

**(scaled with the relic density)**

Relic density depends on  $g_{Z\tilde{\chi}_1^0\tilde{\chi}_1^0}$  in Z-funnel and  $g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0}$  in  $h$ -funnel

**ALLOWED POINTS IN  $\mu < 0$  WITH LIGHT HIGGSINOS**

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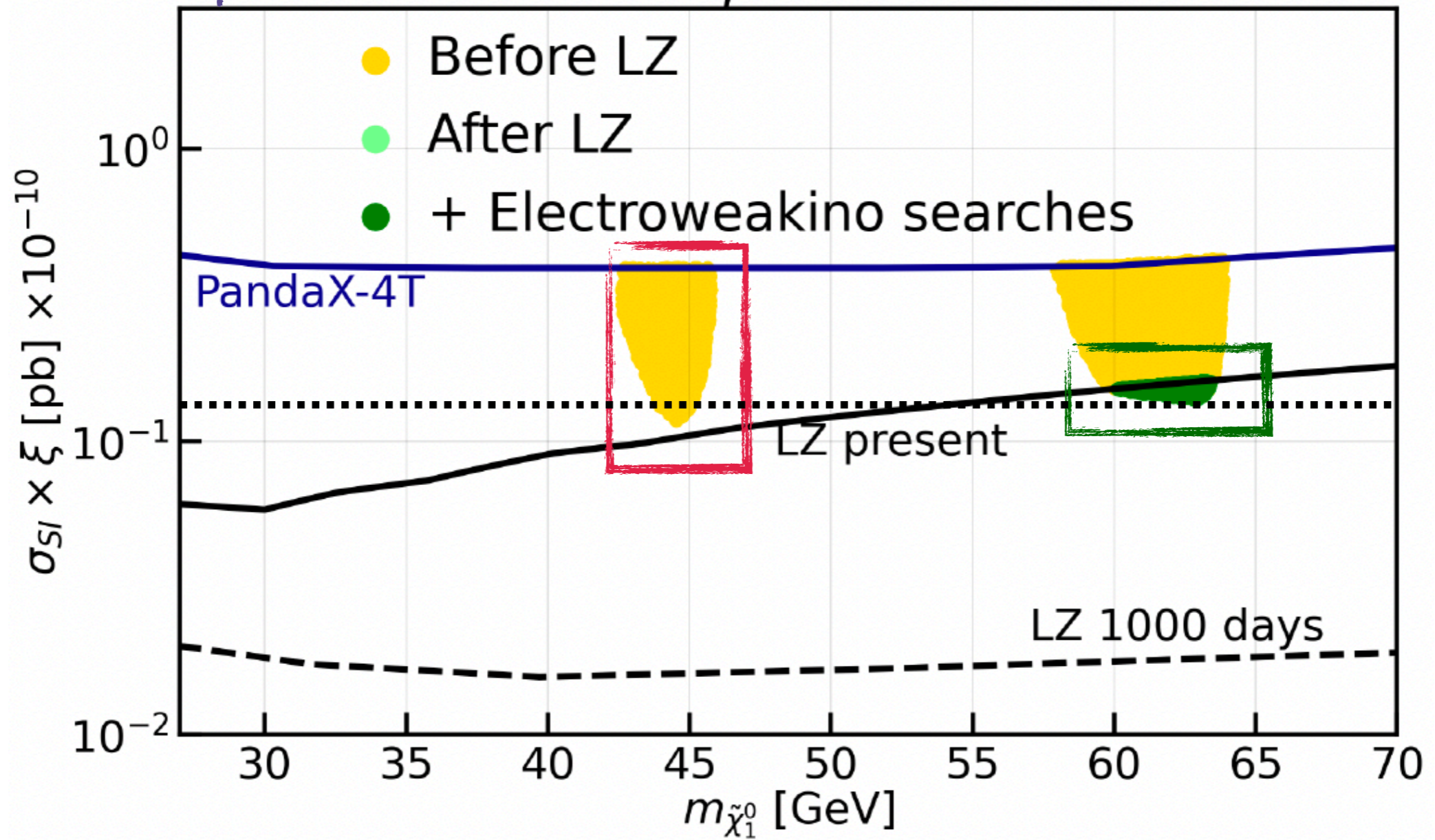
**Can we tune the parameters to  
evade the constraints?**

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# Revisit

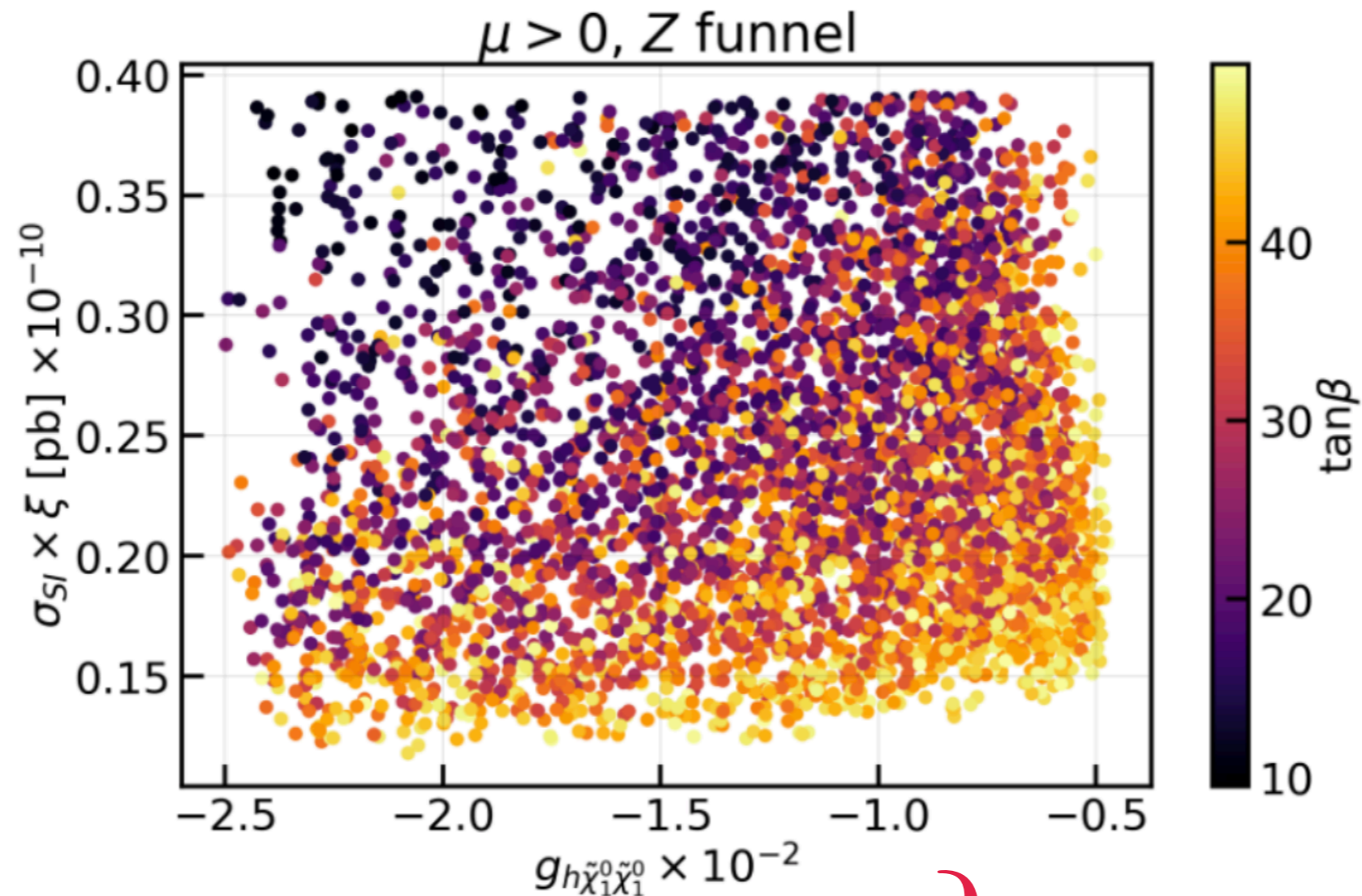
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# The Z-funnel for $\mu > 0$



Low  $\tan\beta$  : High magnitude of  $g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0}$

High  $\tan\beta$  : Low magnitude of  $g_{h\tilde{\chi}_1^0\tilde{\chi}_1^0}$ ,

but added contribution from  $g_{H\tilde{\chi}_1^0\tilde{\chi}_1^0}$

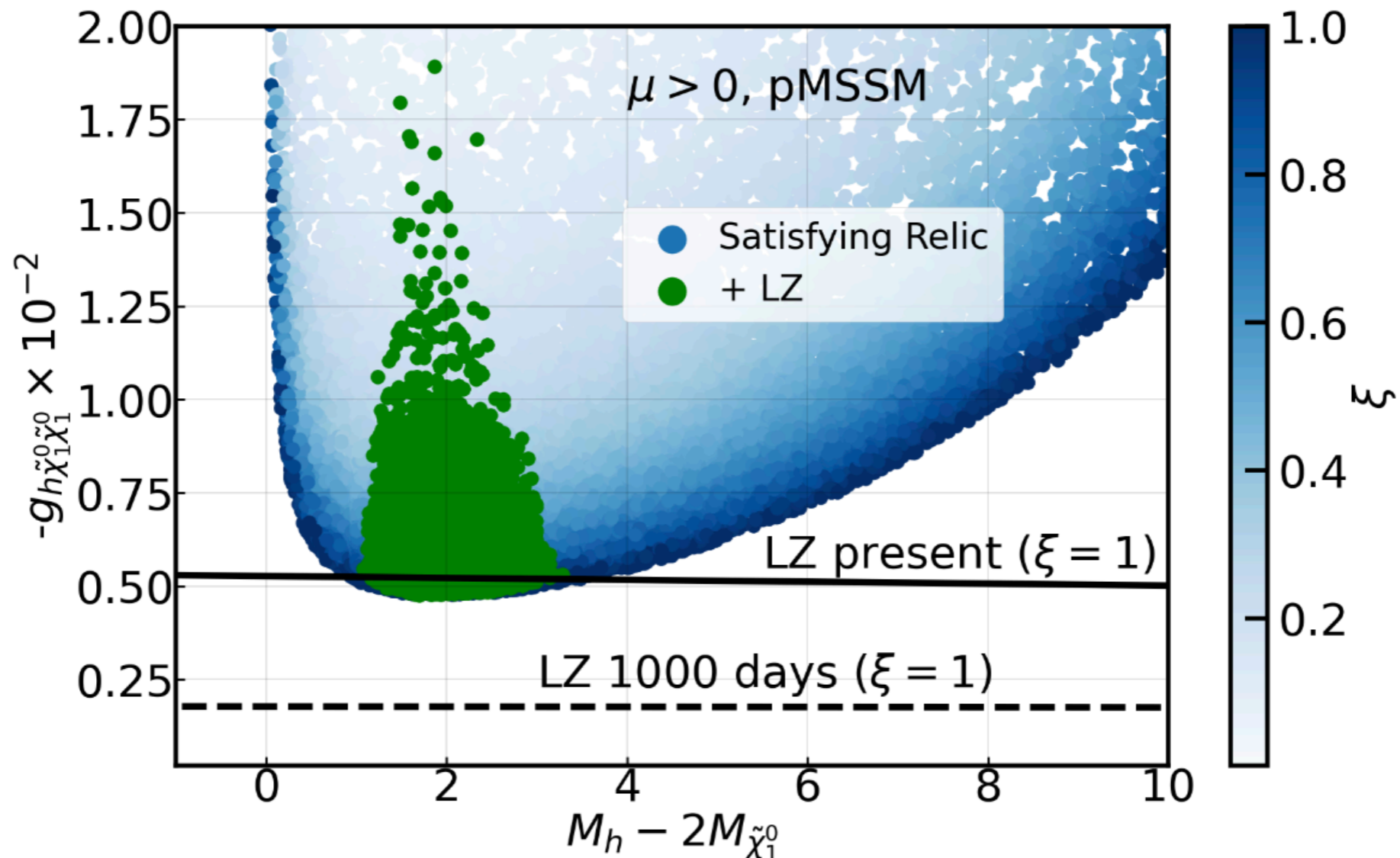
Z-FUNNEL  
EXCLUDED BY LZ

EXCLUDED BY  
ELECTROWEAKINO SEARCHES

Taking into account 20% theoretical uncertainty in relic density - a small allowed region opens up after LZ

# The $h$ -funnel for $\mu > 0$

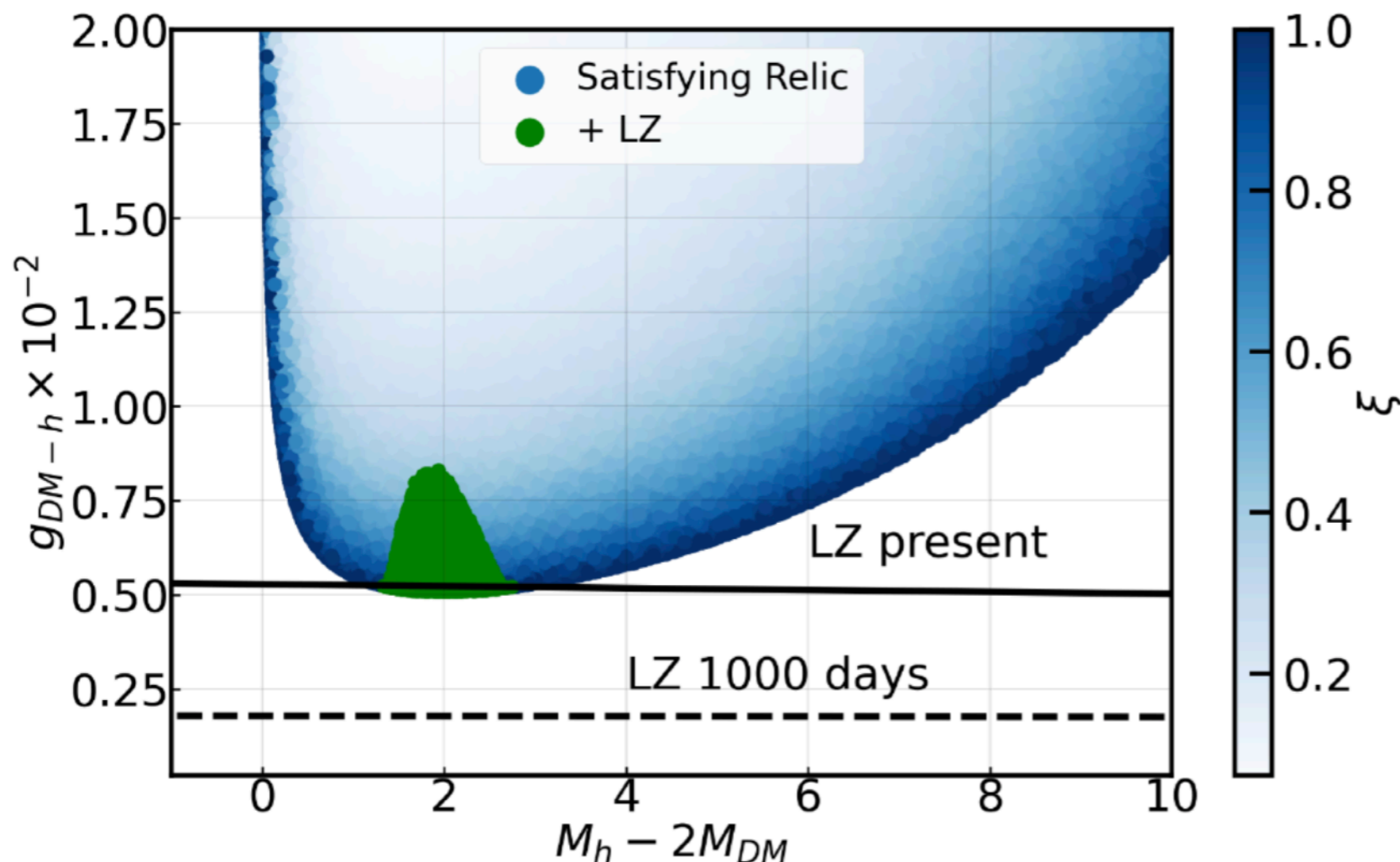
- Heavy higgsino have low values of couplings of LSP with  $Z$  and  $h$ 
  - relic density condition not satisfied
- In  $h$ -funnel, extra handle of  $\tan\beta$ 
  - relic satisfied only for low  $\tan\beta$  where coupling is high
- Effect of  $H$  not important



# Heavy higgsinos in the $h$ -funnel

- Heavy higgsino have low values of couplings of LSP with  $Z$  and  $h$ 
  - relic density condition not satisfied
- In  $h$ -funnel, extra handle of  $\tan\beta$ 
  - relic satisfied only for low  $\tan\beta$  where coupling is high
- Effect of  $H$  not important

Similar to any Majorana fermion coupled to only  $h$



**ALSO STRONGLY  
CONSTRAINED**

Can be probed with few  
more days of LZ data

# Light higgsinos still allowed by electroweakino searches?

Light higgsinos survive in the region where

$$M_{\tilde{\chi}_1^\pm/\tilde{\chi}_2^0/\tilde{\chi}_3^0} - M_{\tilde{\chi}_1^0} \approx M_Z$$

Performed an analysis with leptonic final states using XGBOOST

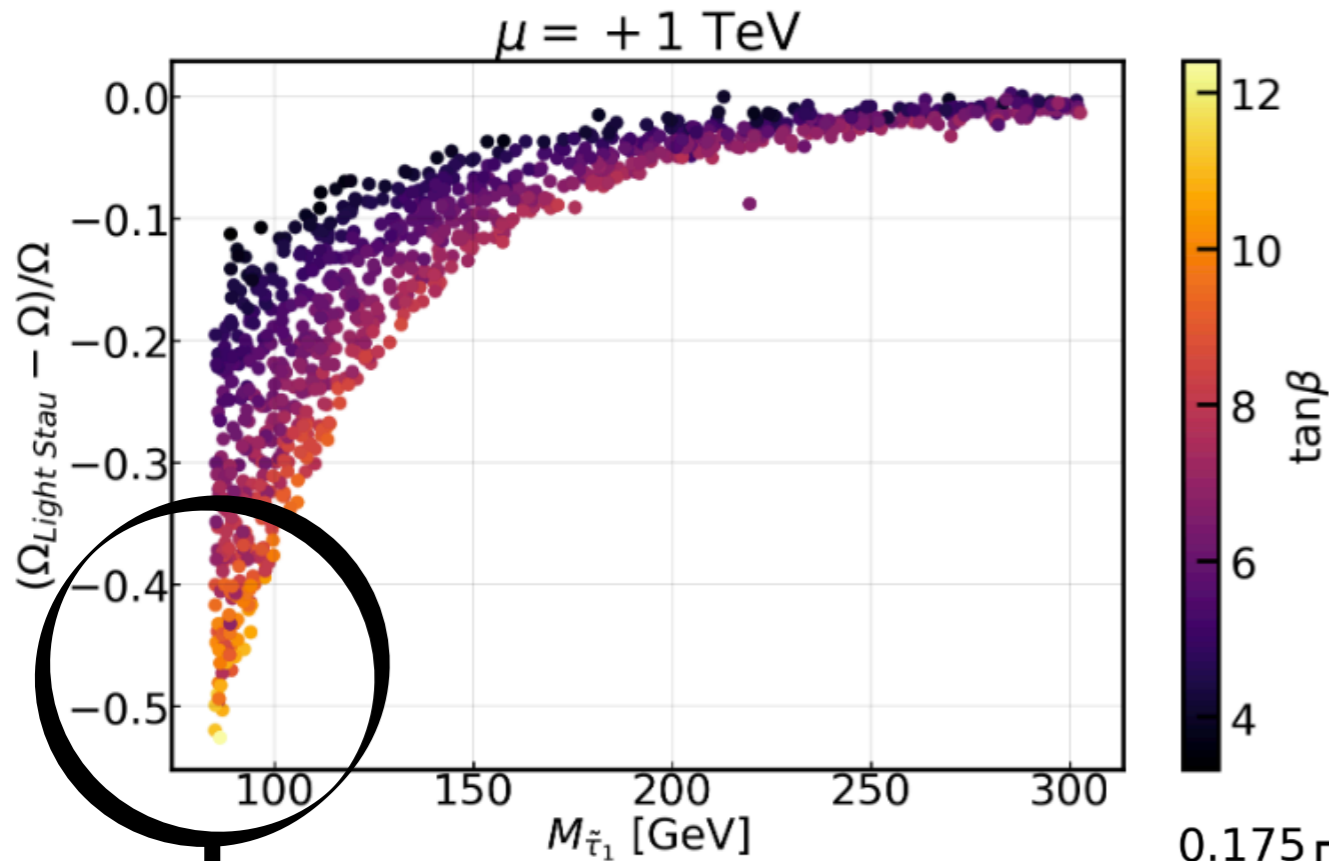
Signal significance of 3.6 (1.5) with 20% (50%)  
systematic uncertainty with  $137 \text{ fb}^{-1}$  of data at 14 TeV

Could be probed with upcoming analyses of the Run-2 data  
which have not yet been implemented in SModelS  
or in the **Run-3 of LHC**

Experimental collaborations need to focus on this region of  
light higgsinos to **provide a conclusive statement about  
their present status.**

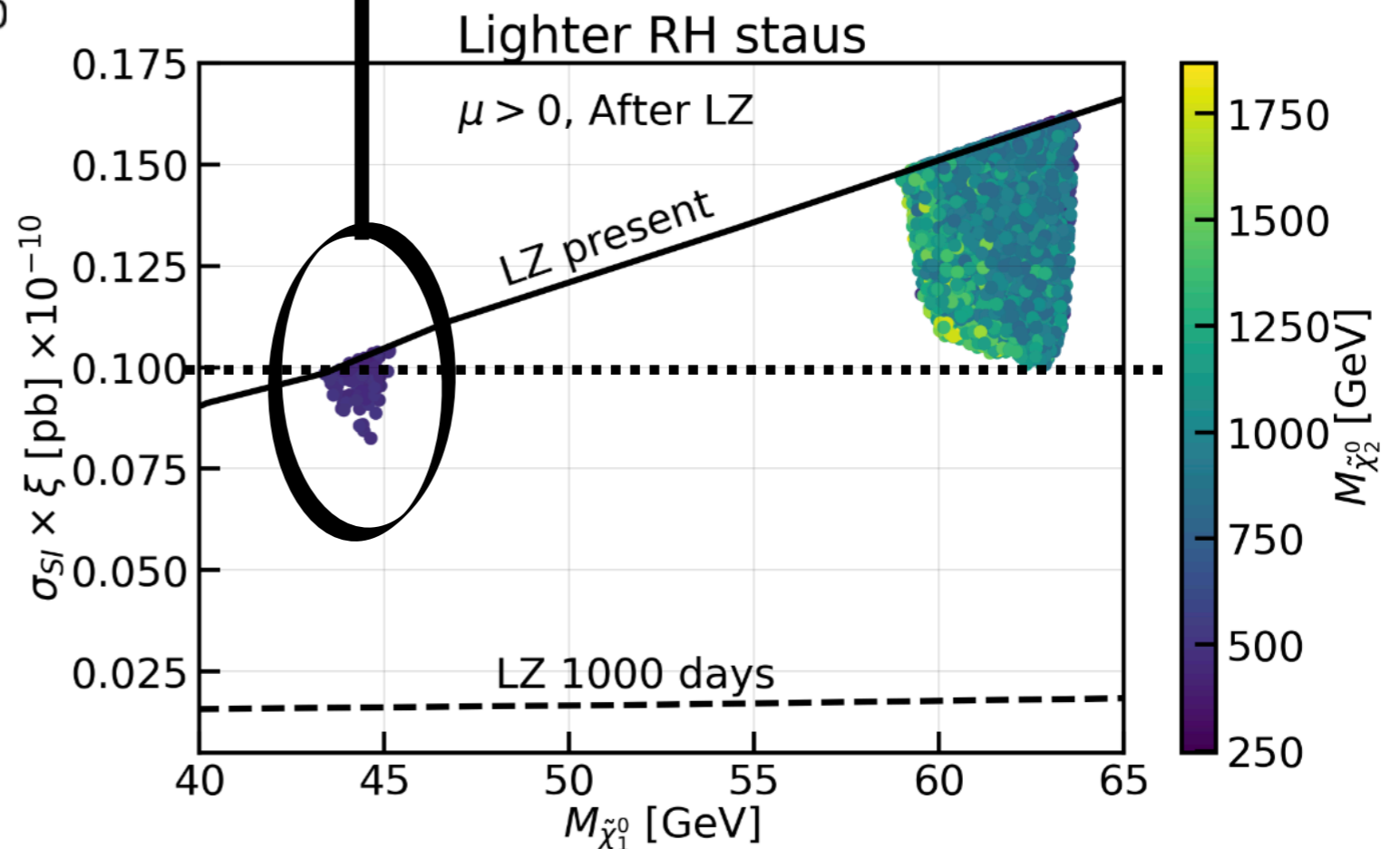


# Caveat: Light staus

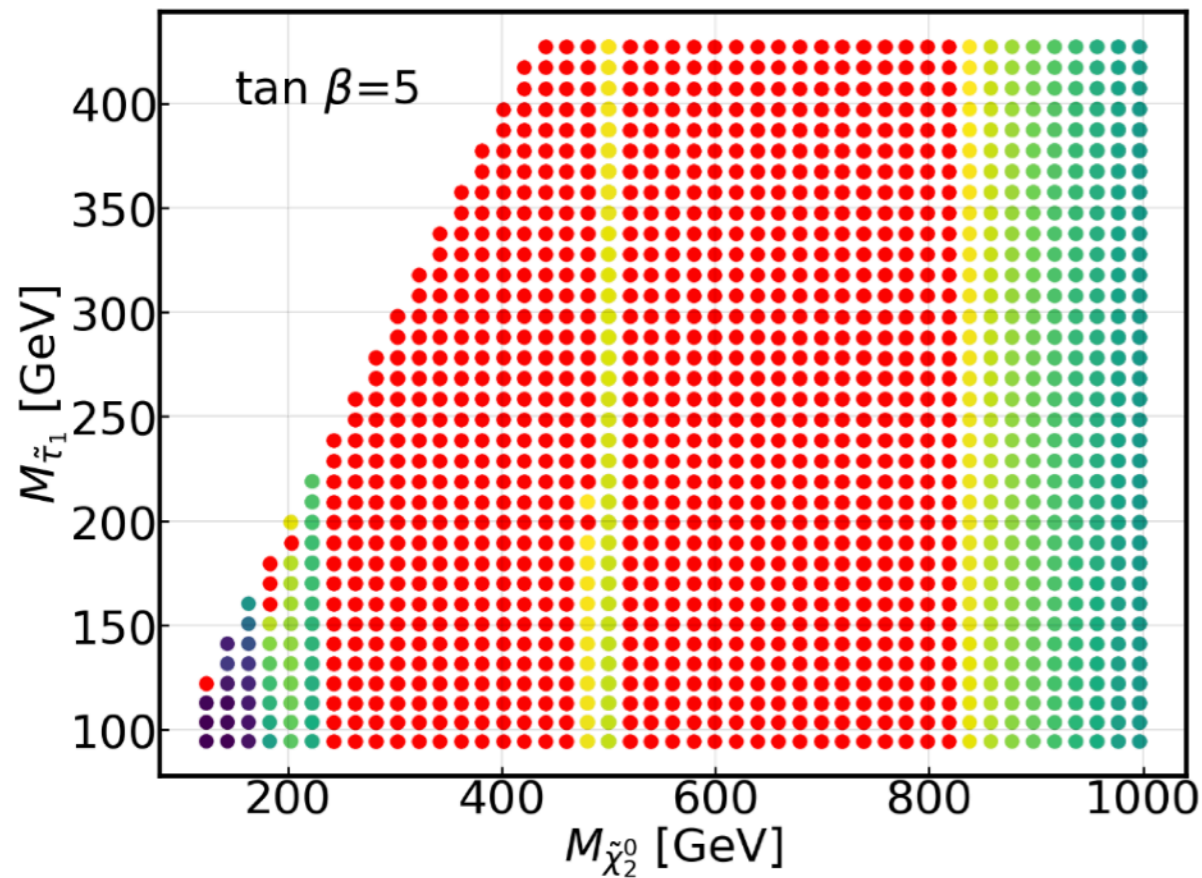


A region in the  $Z$ -funnel open up  
and in the  $h$ -funnel, we can go to  
lower DD cross-sections  
- can be probed by full run of LZ

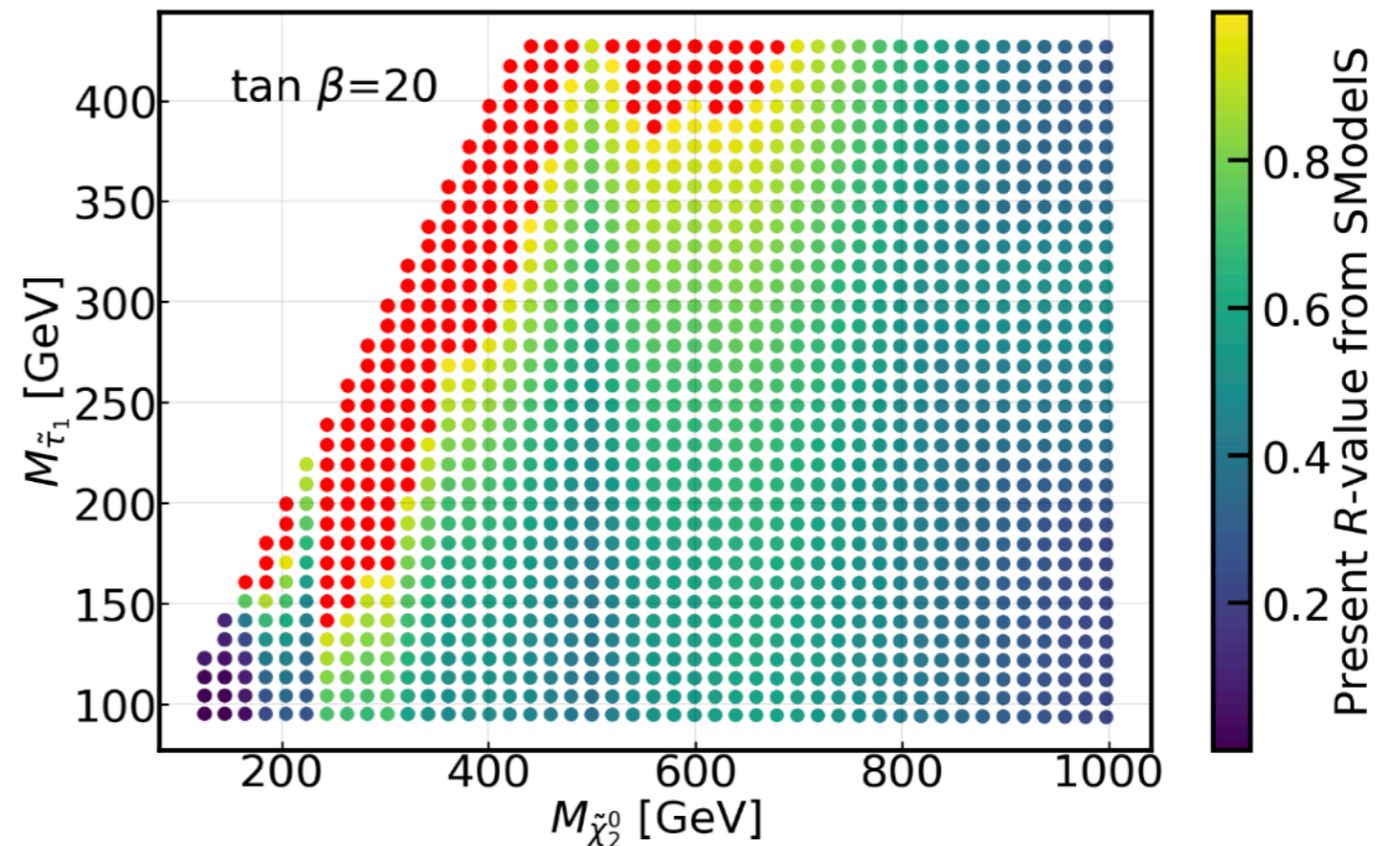
Below 100 GeV, the relic  
density can be reduced by  
50% in the presence of a  
90-95 GeV RH stau



# Caveat: Light staus



**Red regions:** Excluded by present searches implemented in SModels



Limits on Higgsinos weaken when their branching to staus increases

New regions of parameter space open - can be probed at LHC Run-3

# Summary

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The current experiments, especially the **recent results from the electroweakino searches at the LHC** and the **LZ dark matter DD experiment** have squeezed the allowed parameter space to regions which can either be

- regions of **heavy higgsinos** very close to being probed by few days of **LZ** data
- contain very low mass higgsinos which can be targeted at the **Run-3 of LHC** with dedicated analyses **to be sensitive in this narrow gap**.

In the presence of **light staus**, extra regions of parameter space open up

- due to reduced relic density
- relaxed collider constraints when higgsinos decay to stau

These regions are also within the reach of the **LZ experiment and the LHC Run-3**.

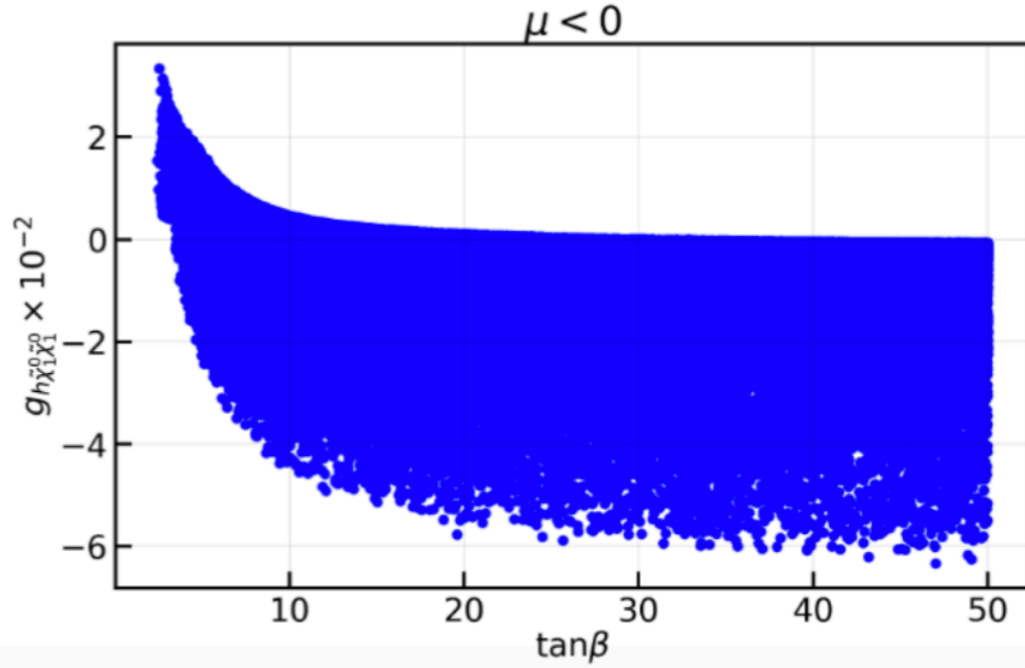
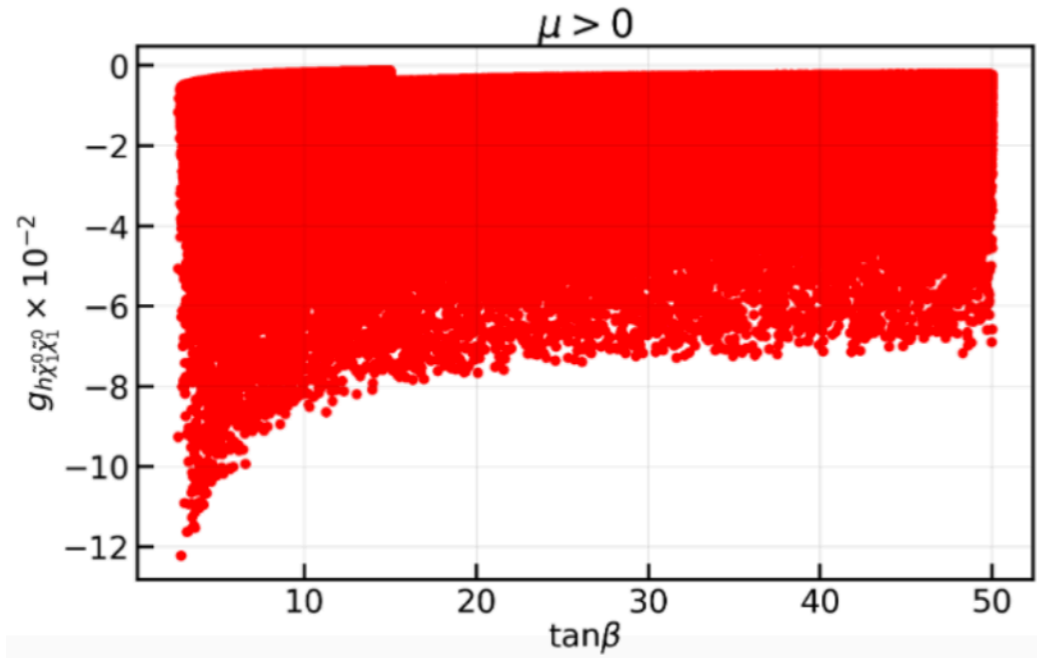
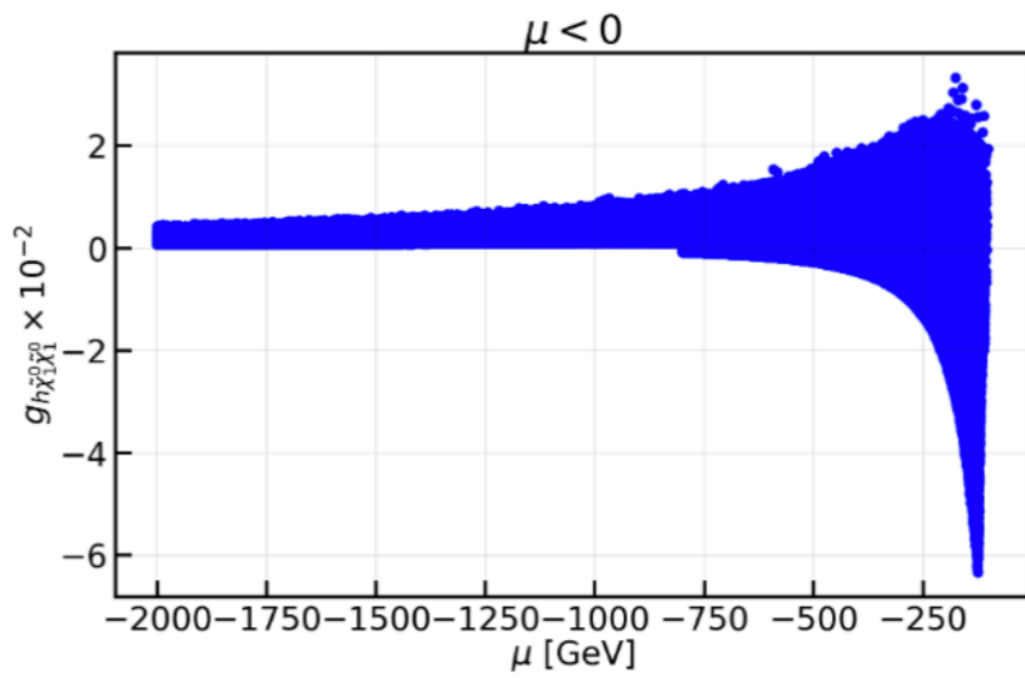
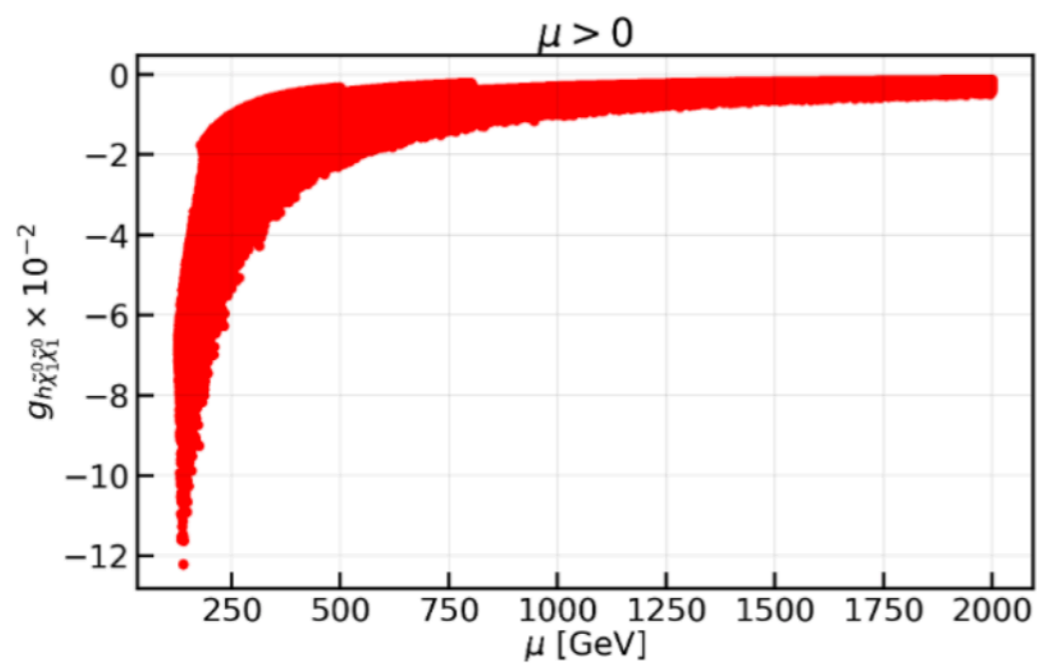
# Takeaway message

**How does this very conventional dark matter candidate stand against the recent experimental results?**

At present, we are at a very exciting juncture where the *experiments lined up might exclude the possibility of a light neutralino thermal DM in pMSSM altogether,* or we might be *very close to start observing the first hints of new physics.*

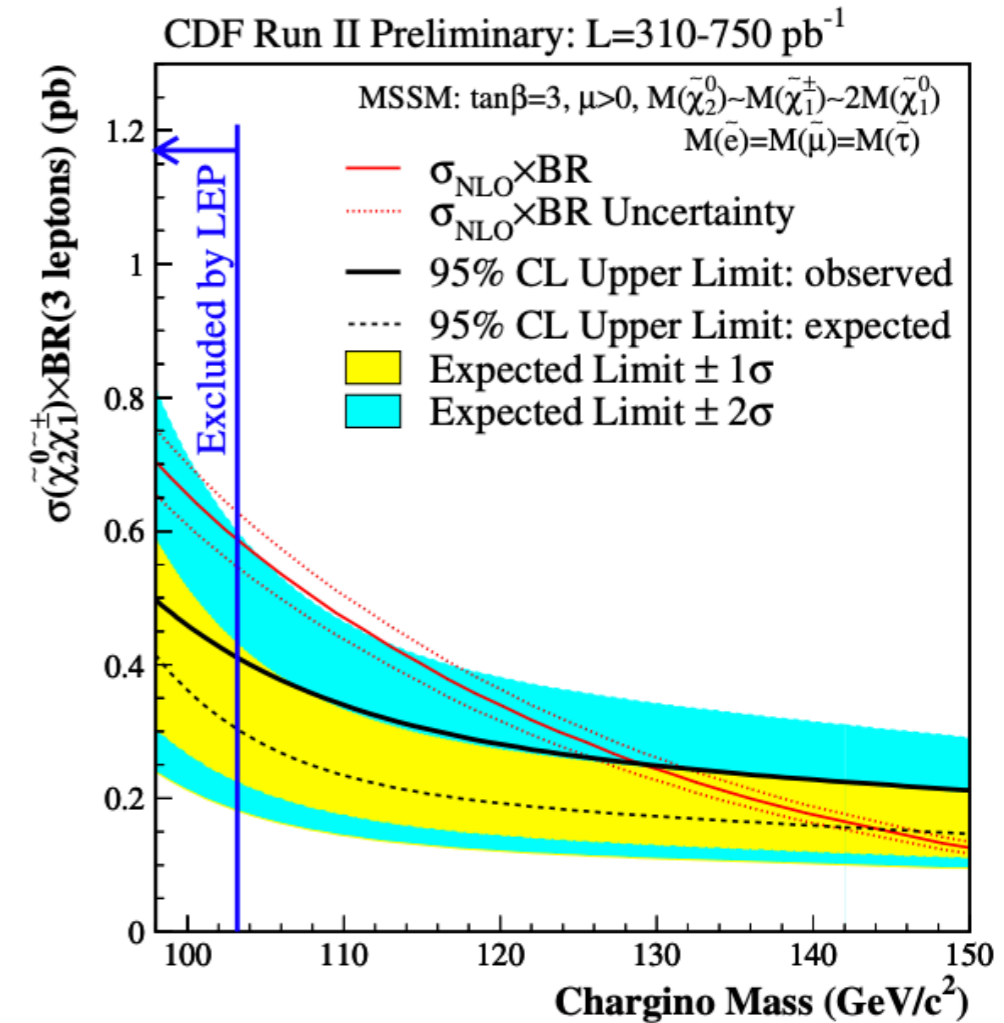
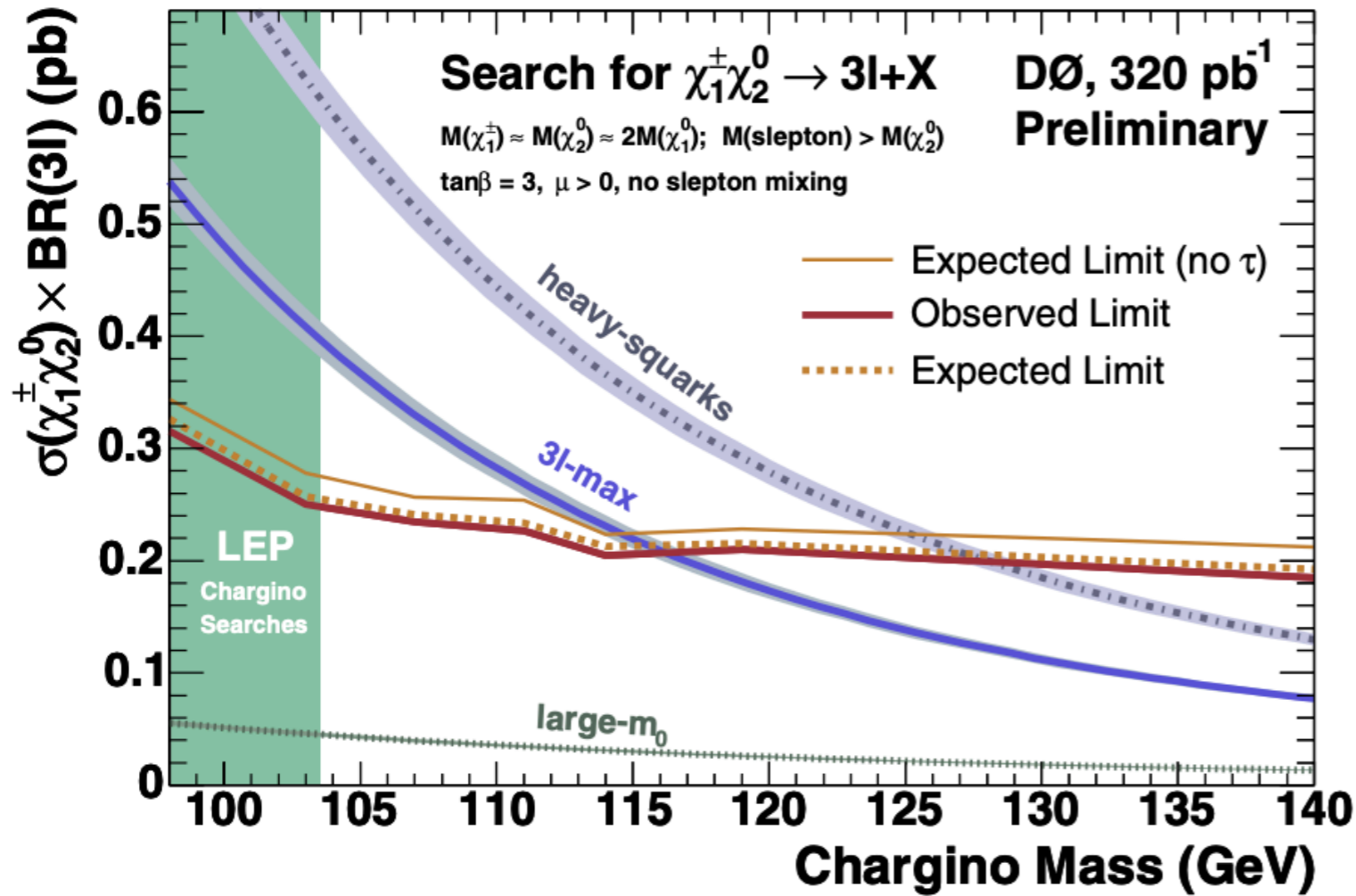
*Thank you for your attention*

Back up slides



Benchmarks ( <i>mass parameters in GeV</i> )			$m_h[\Delta_{M_h}^{FH}]$ [GeV]	$\sigma_{SI} \times \xi \times 10^{-10}$ [pb]
$\mu > 0$	<i>h</i> -funnel	$M_t = 173.21, M_1 = 62.5, M_2 = 2000, \mu = 1000, \tan\beta = 5, M_A = 3000, M_{\tilde{Q}_{3L}} = 10000, M_{\tilde{t}_R} = 10000, M_{\tilde{b}_R} = 10000, A_t = 10000, M_3 = 3000$	125.38 [ $\pm 0.97$ ]	0.151
$\mu < 0$	Z-funnel	$M_t = 173.21, M_1 = 44, M_2 = 2000, \mu = -124, \tan\beta = 5, M_A = 3000, M_{\tilde{Q}_{3L}} = 10000, M_{\tilde{t}_R} = 10000, M_{\tilde{b}_R} = 10000, A_t = 10000, M_3 = 3000$	125.88 [ $\pm 0.96$ ]	$0.746 \times 10^{-3}$
	<i>h</i> -funnel	$M_t = 173.21, M_1 = 68, M_2 = 2000, \mu = -150, \tan\beta = 50, M_A = 3000, M_{\tilde{Q}_{3L}} = 5000, M_{\tilde{t}_R} = 5000, M_{\tilde{b}_R} = 5000, A_t = -5000, M_3 = 3000$	125.67 [ $\pm 0.63$ ]	0.143
		$M_t = 173.21, M_1 =, M_2 = 2000, \mu = -1000, \tan\beta = 4.5, M_A = 3000, M_{\tilde{Q}_{3L}} = 10000, M_{\tilde{t}_R} = 10000, M_{\tilde{b}_R} = 10000, A_t = 10000, M_3 = 3000$	125.15 [ $\pm 0.99$ ]	0.150

# Tevatron Limit



Beyond the Standard Model physics at the Tevatron,  
 Mario P Giordani 2006 J. Phys.: Conf. Ser. 53 329

# XGBOOST analysis

Final state: 3l+MET  
No SFOS pair of leptons

Backgrounds:  $lll\nu$  ( $l \equiv e, \mu, \tau$ ),  $ZZ, t\bar{t}, VVV,$   
 $Wh, Zh,$  ggF and VBF production of  $h$  with  $h \rightarrow ZZ^*,$   
 $t\bar{t}h, t\bar{t}W,$  and  $t\bar{t}Z$

exactly three leptons satisfying  $p_T > 25, 25, 20$  GeV and  $|\eta| < 2.4,$   
a veto on  $b$ -jets with  $p_T > 30$  GeV and  $|\eta| < 2.5.$

- Transverse momenta ( $p_T$ ) of the three leptons
- Transverse mass ( $M_T$ ) and contranverse mass ( $M_{CT}$ ) of each of the three leptons with the  $\cancel{E}_T$
- Minimum and maximum values of  $\Delta R$  between opposite sign lepton pairs along with their  $\Delta\eta$  values
- Invariant mass of the opposite sign lepton pairs with minimum and maximum  $\Delta R$
- Missing transverse momentum
- Number of jets in the event with the  $p_T$  of the two leading jets
- Scalar sum of  $p_T$  of all the jets in the event ( $H_T$ )
- Invariant mass of the three leptons

Following are the hyperparameters of the XGBOOST model:

```
'objective': 'multi:softprob', 'colsample_bytree': 0.3, 'learning_rate': 0.1, 'num_class': 12,  
'max_depth': 7, 'alpha': 5, 'eval_metric': 'mlogloss', 'num_round': 1000, 'early_stopping_rounds': 3
```



